

Automatic Generation of Vectorizing Compilers for Customizable Digital Signal Processors

Samuel Thomas, James Bornholt

UT Austin

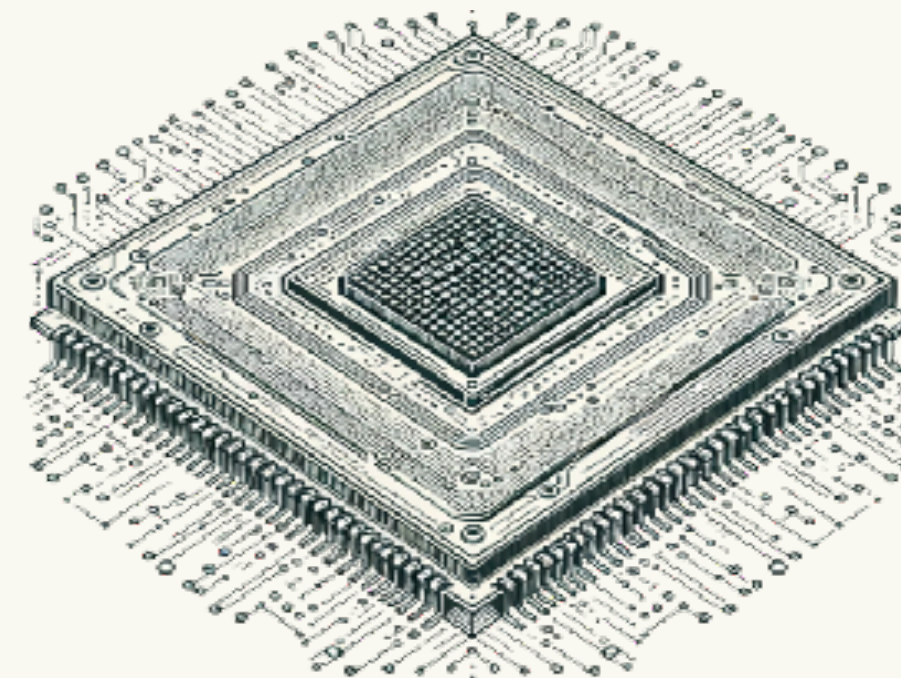
ASPLOS '24



Programmer

```
for i in 0..len(A):  
    C[i] = A[i] + B[i]
```

Vectorizing
Compiler

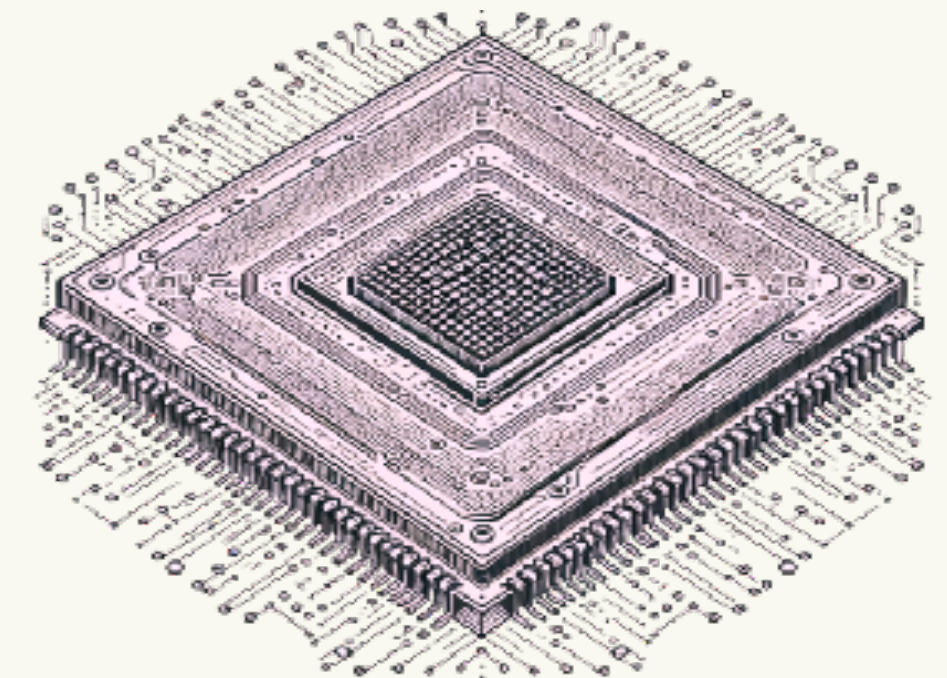
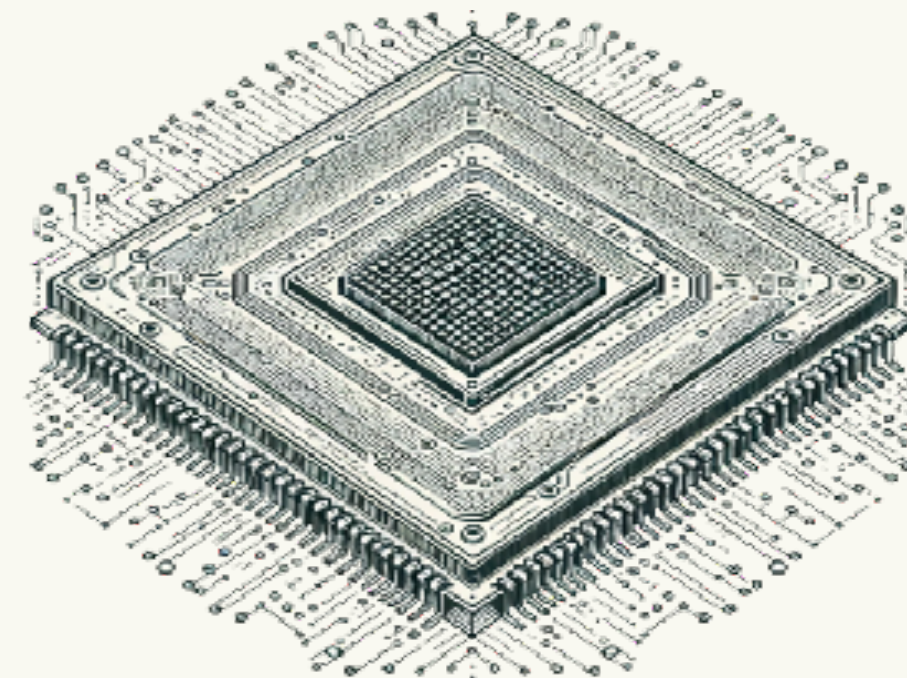
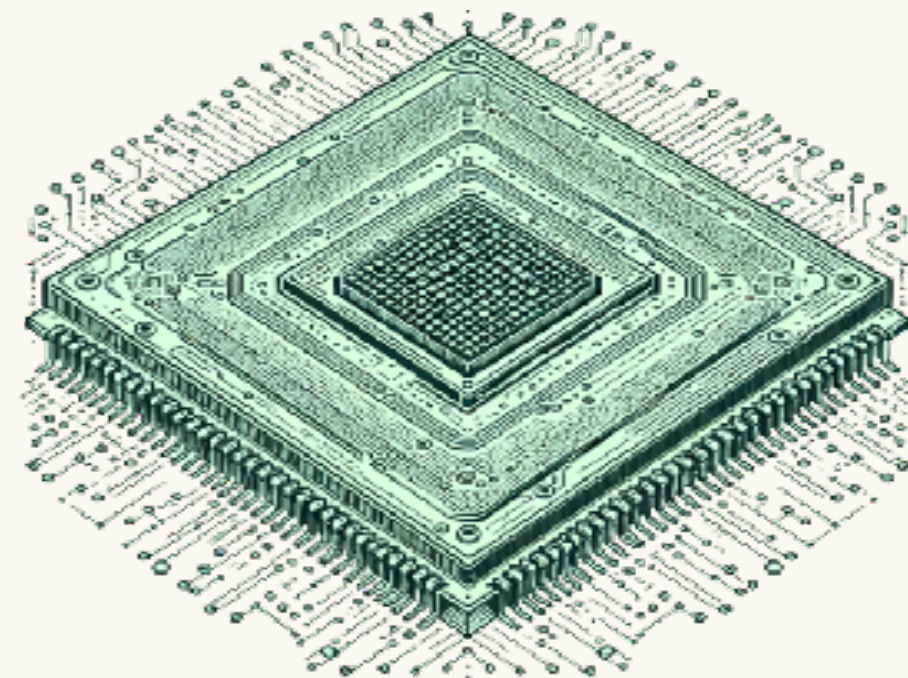


Digital Signal Processor
(DSP)

Programmer

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for i in 0..len(A):  
    C[i] = A[i] + B[i]
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Vectorizing
Compiler



Digital Signal Processor
(DSP)

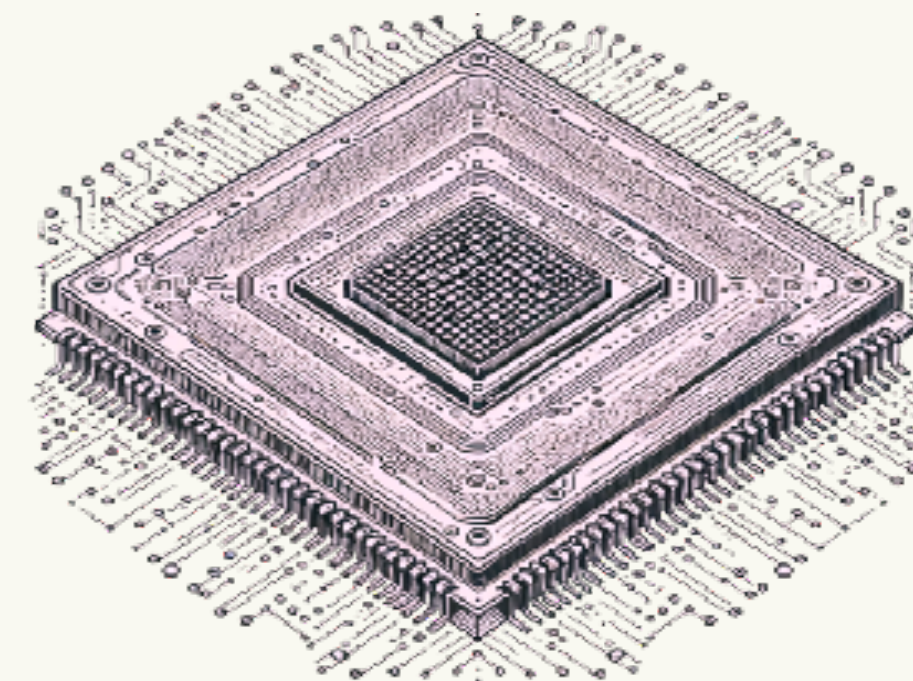
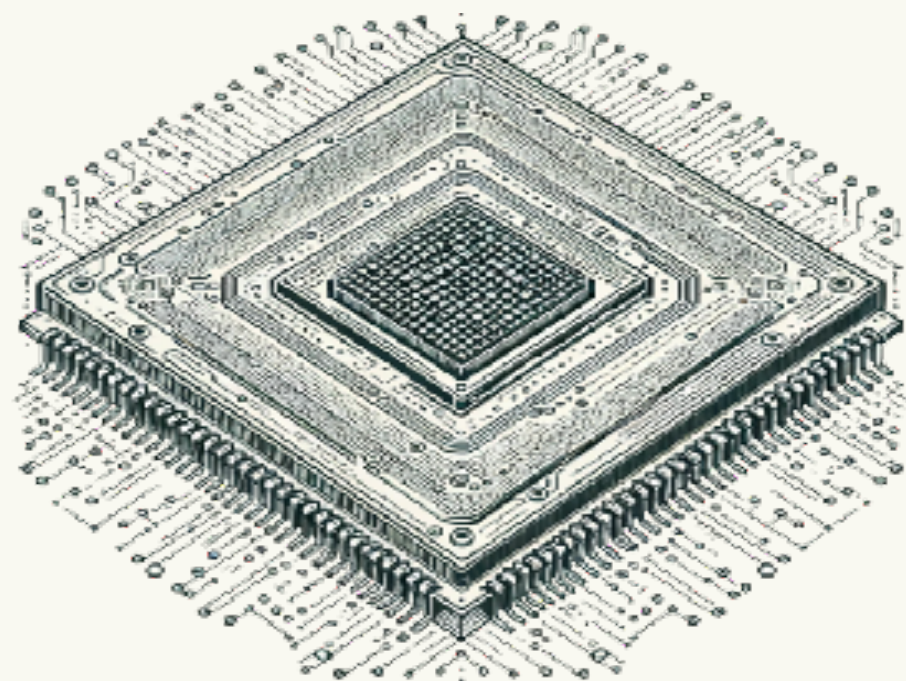
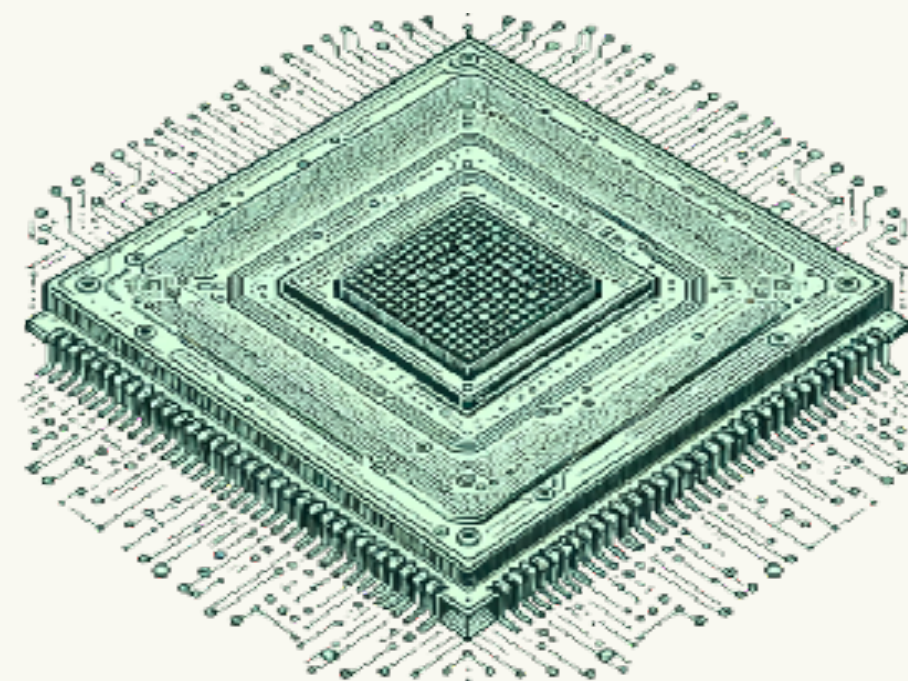
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Vectorizing
Compiler

Vectorizing
Compiler

Vectorizing
Compiler

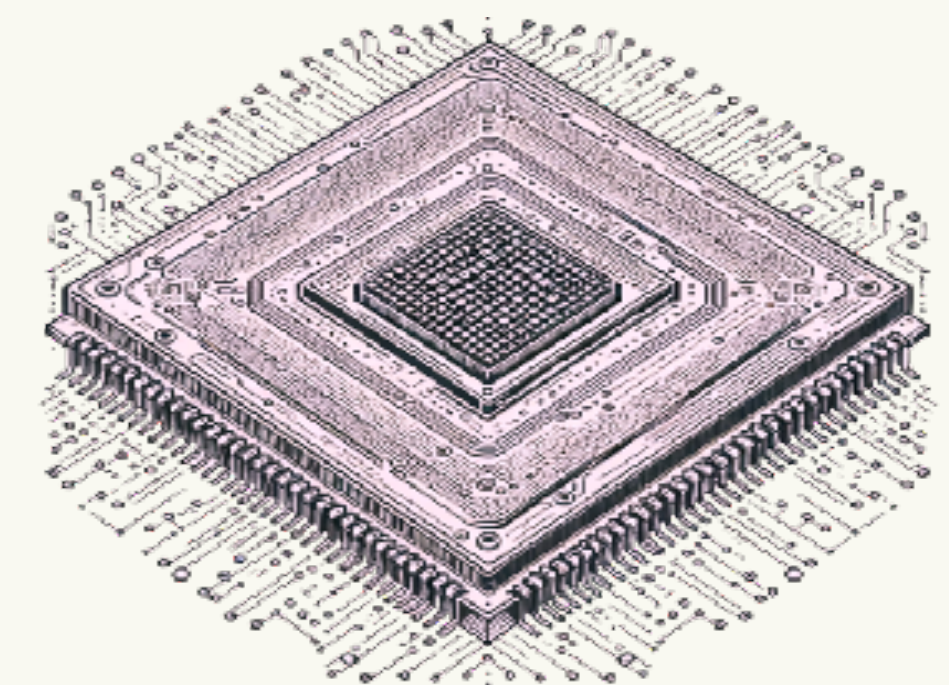
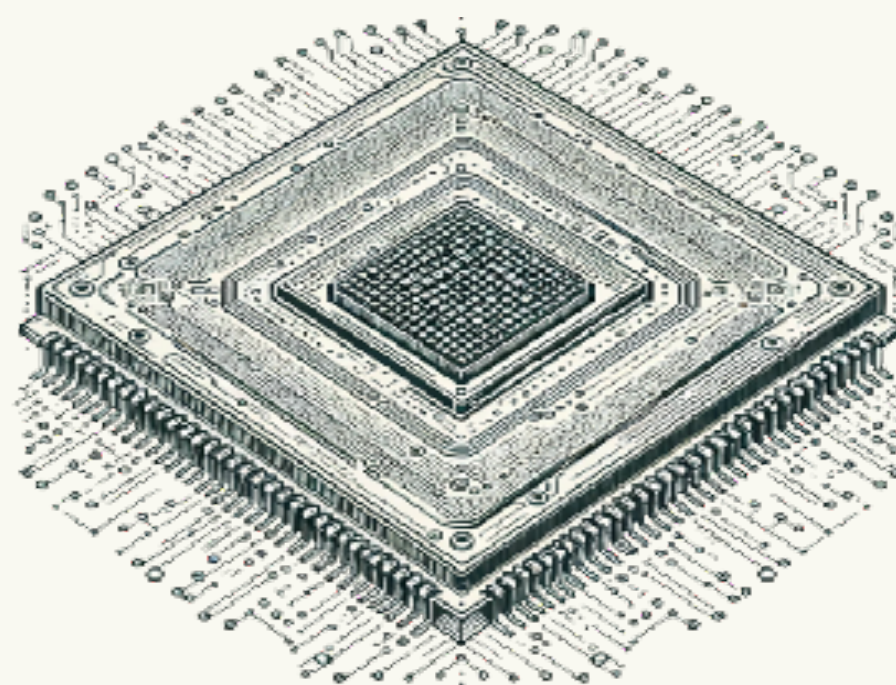
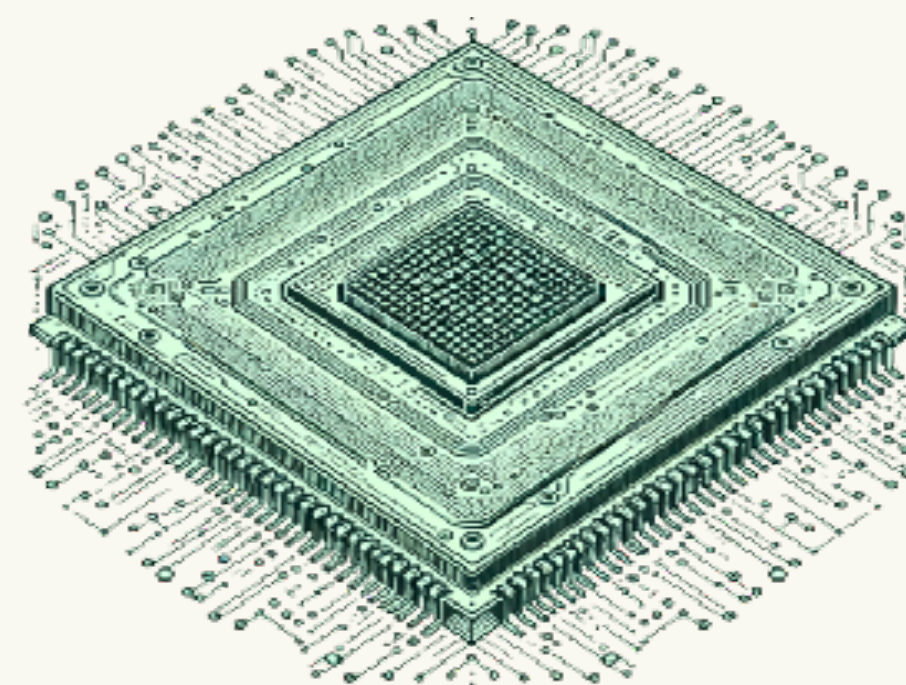
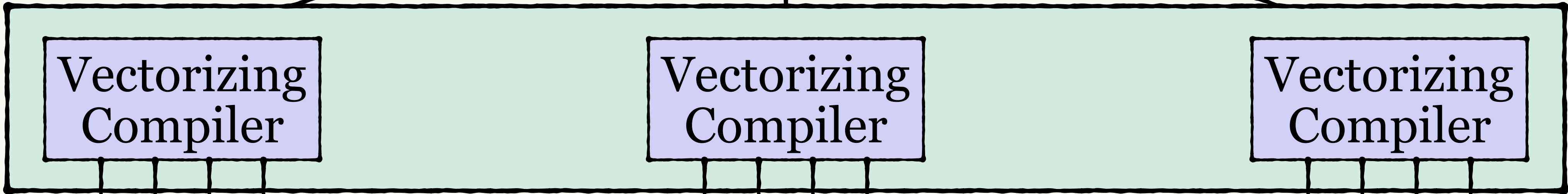


Digital Signal Processor
(DSP)

Programmer

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  C[i] = A[i] + B[i]
```

Automate

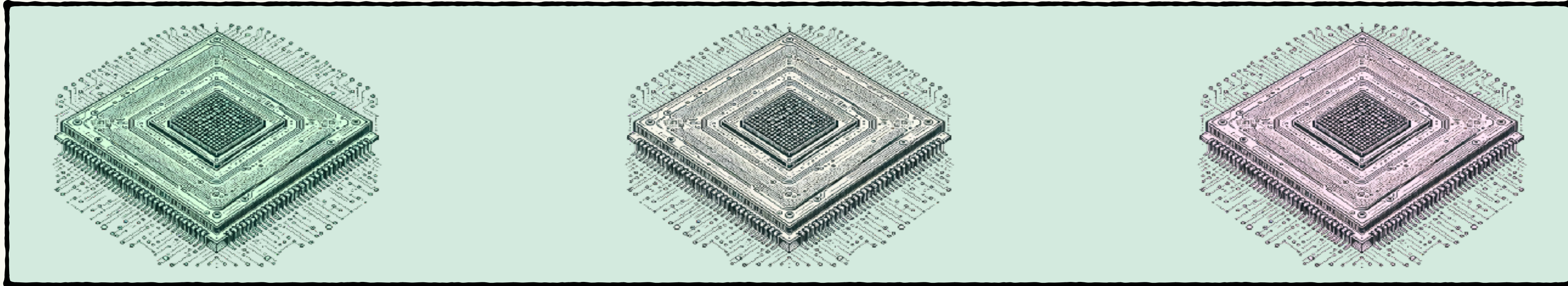
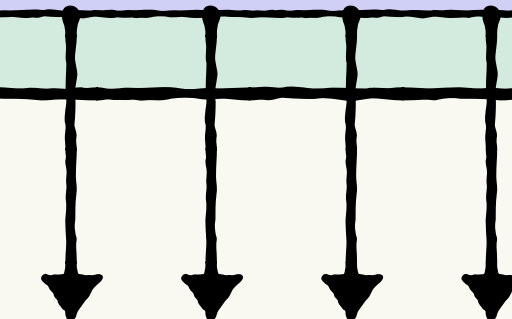
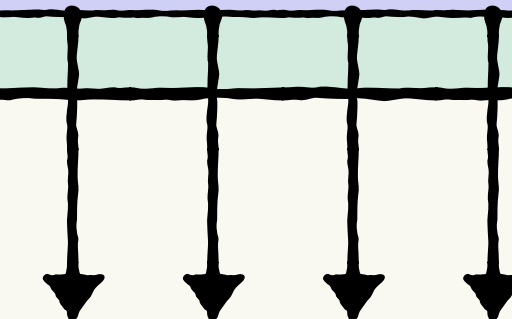
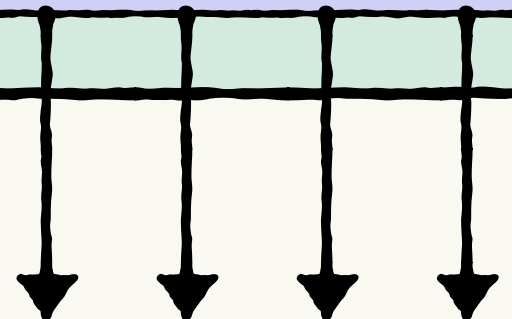
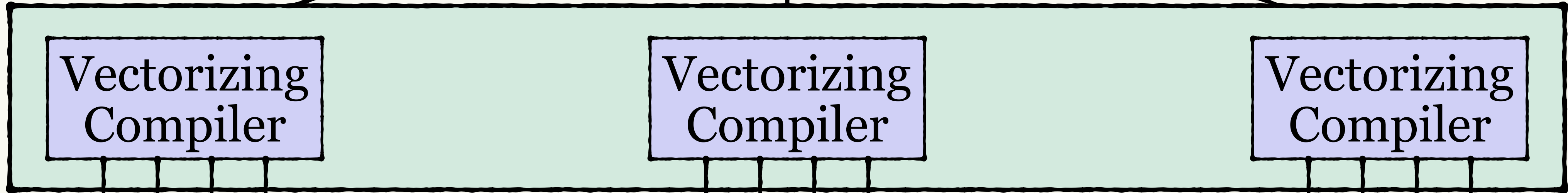


Digital Signal Processor
(DSP)

Programmer

```
for i in 0..len(A):  
  C[i] = A[i] + B[i]
```

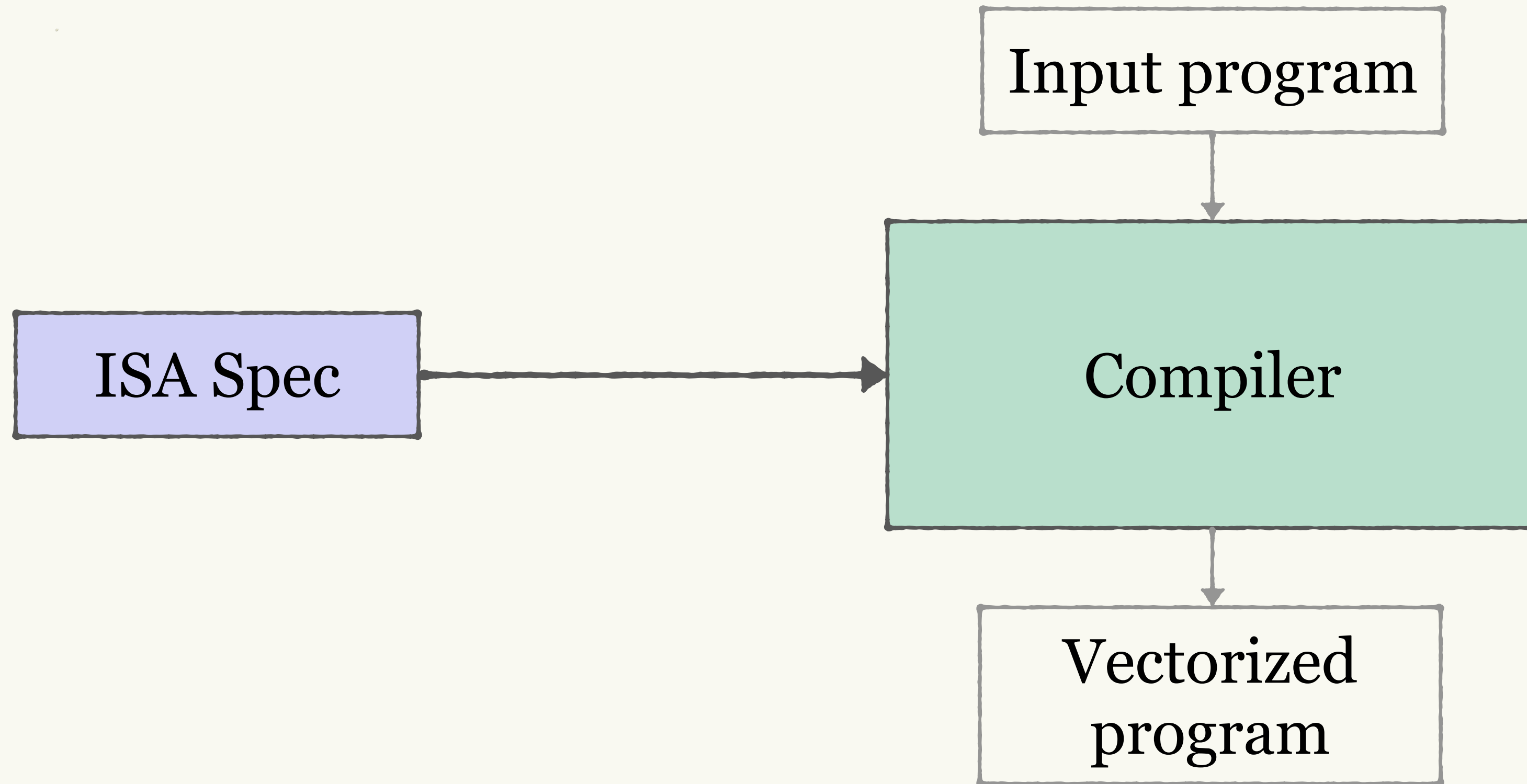
Automate



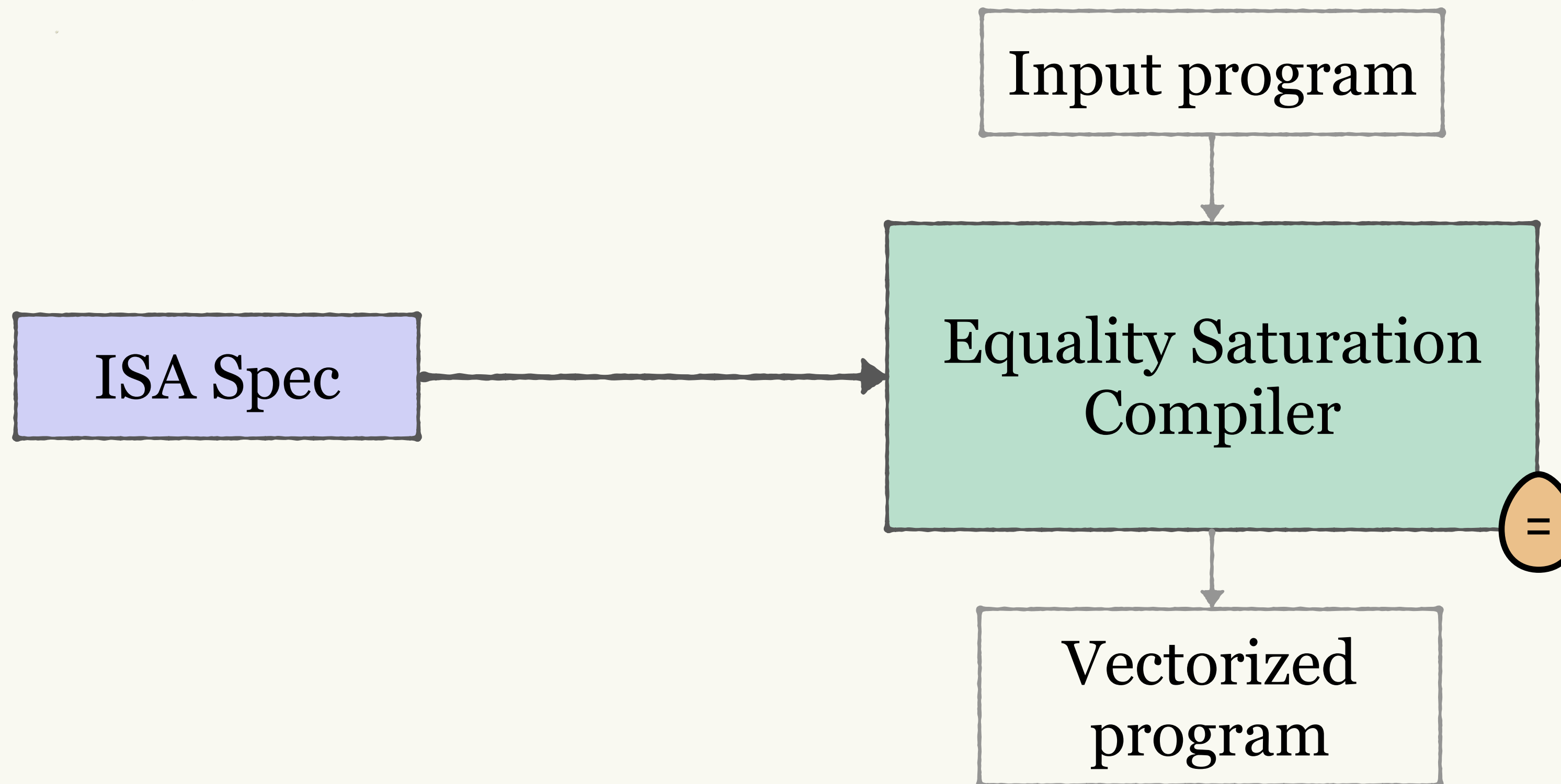
Explore

Digital Signal Processor
(DSP)

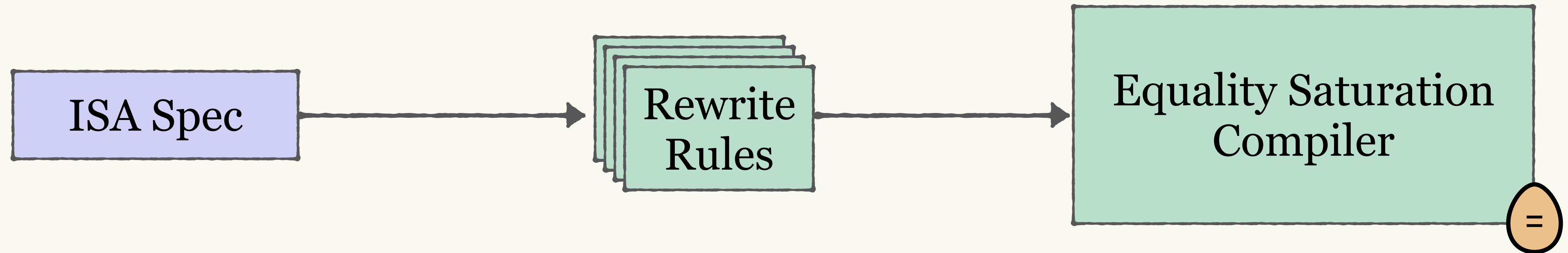
Isaria



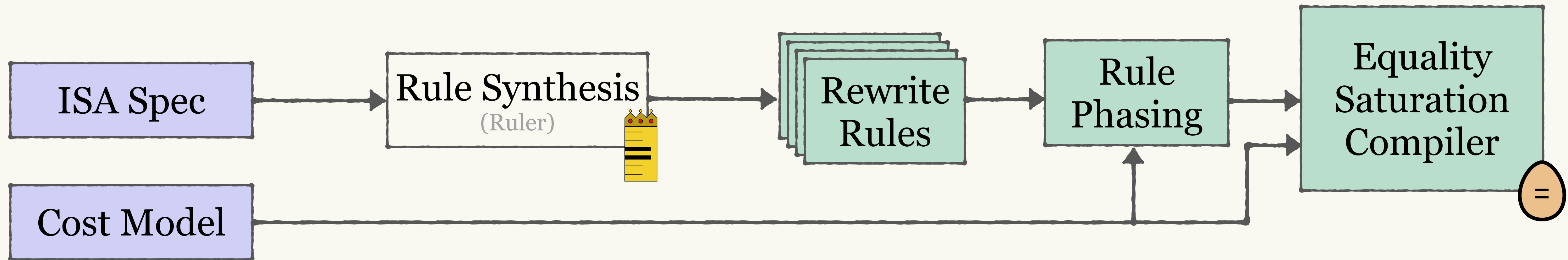
Isaria



Isaria



Isaria

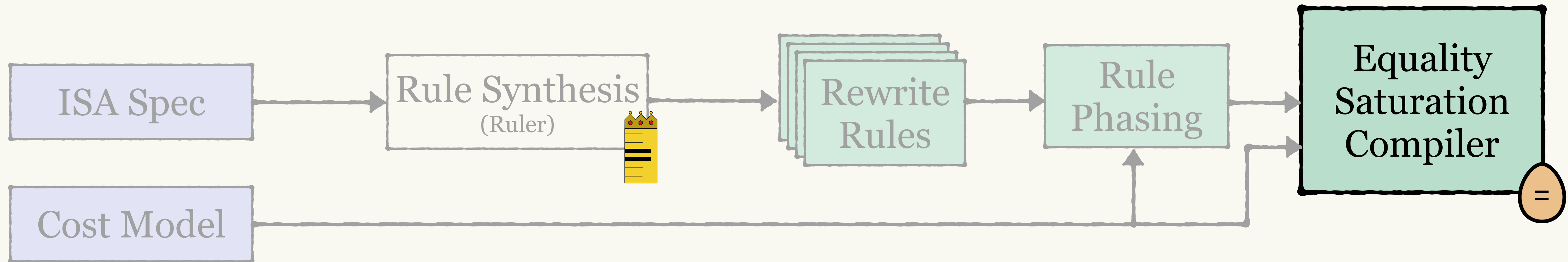


egg: Willsey, et al. (POPL '21)

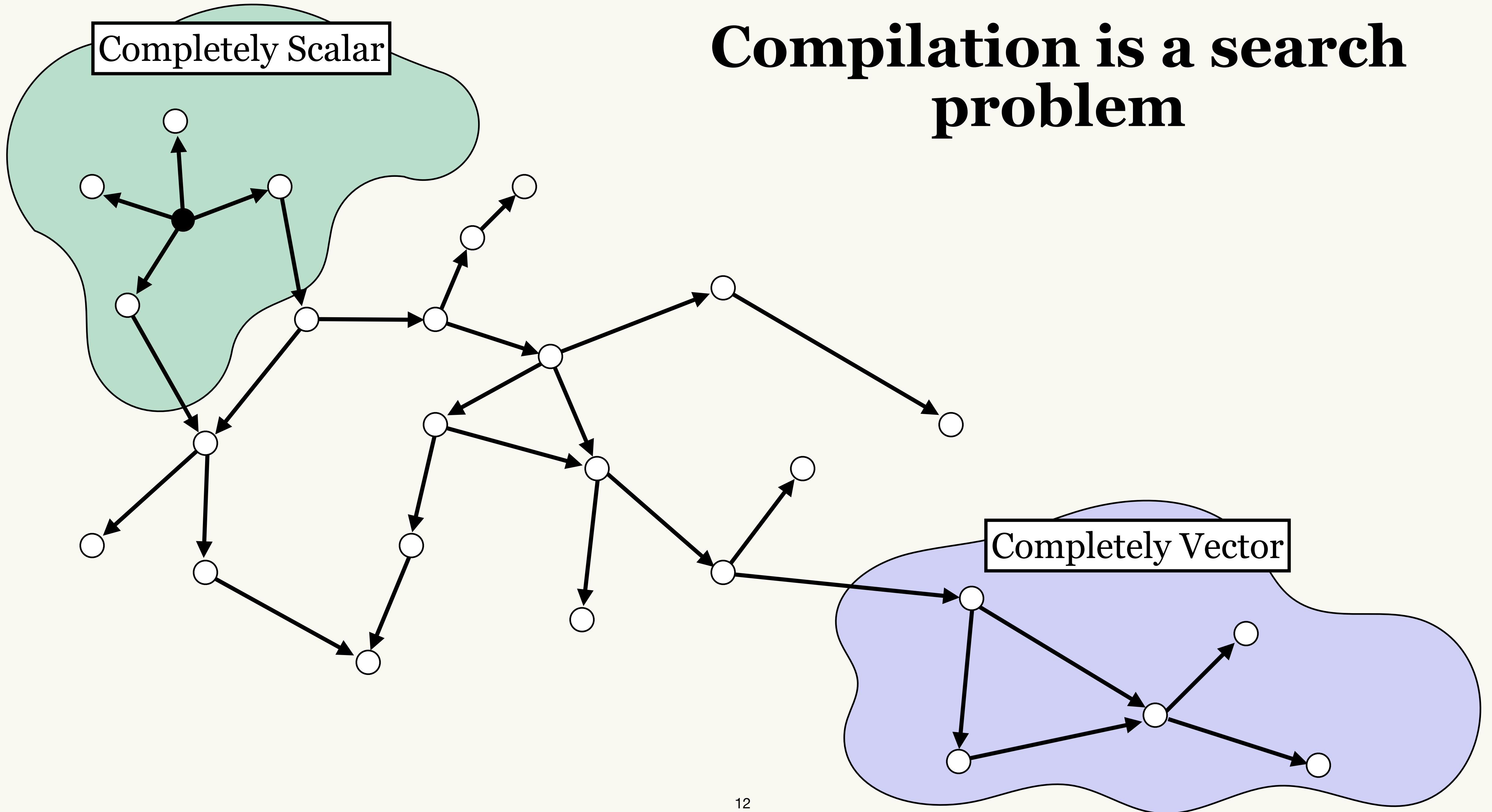
Ruler: Nandi, et al. (OOPSLA '21)

Diospyros: Alexa VanHattum, et al (ASPLOS '21)

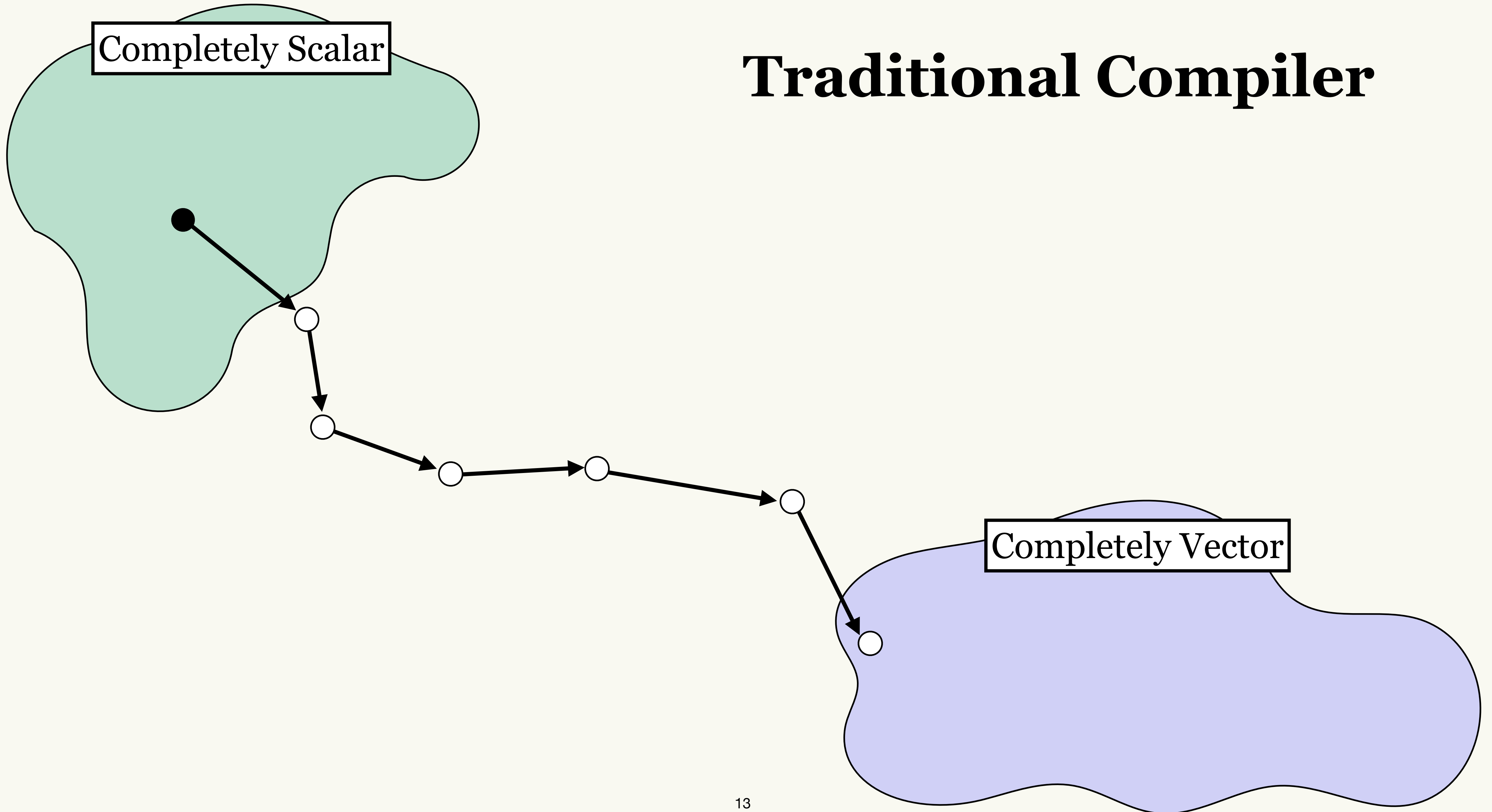
Isaria



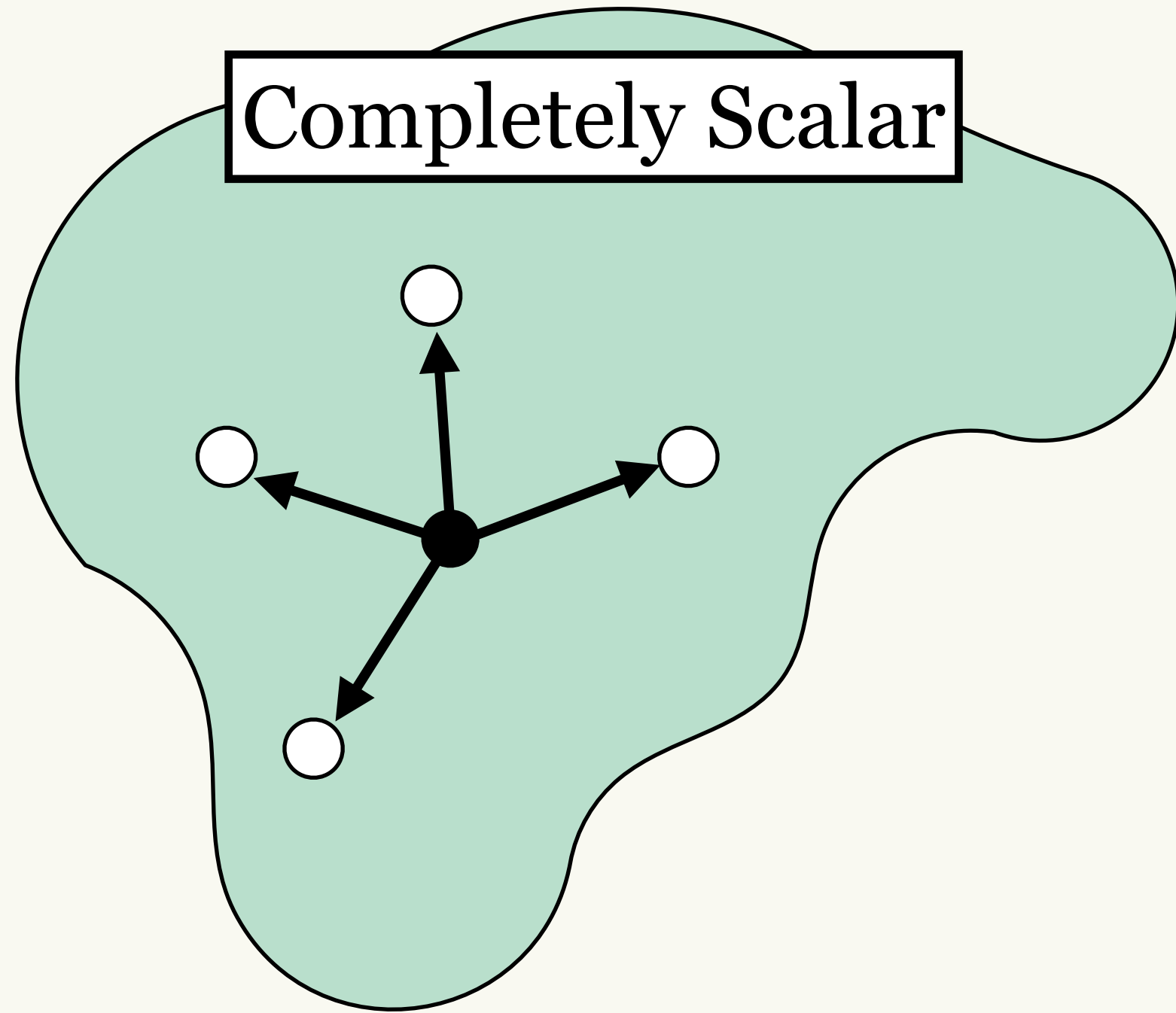
Compilation is a search problem



Traditional Compiler



Completely Scalar



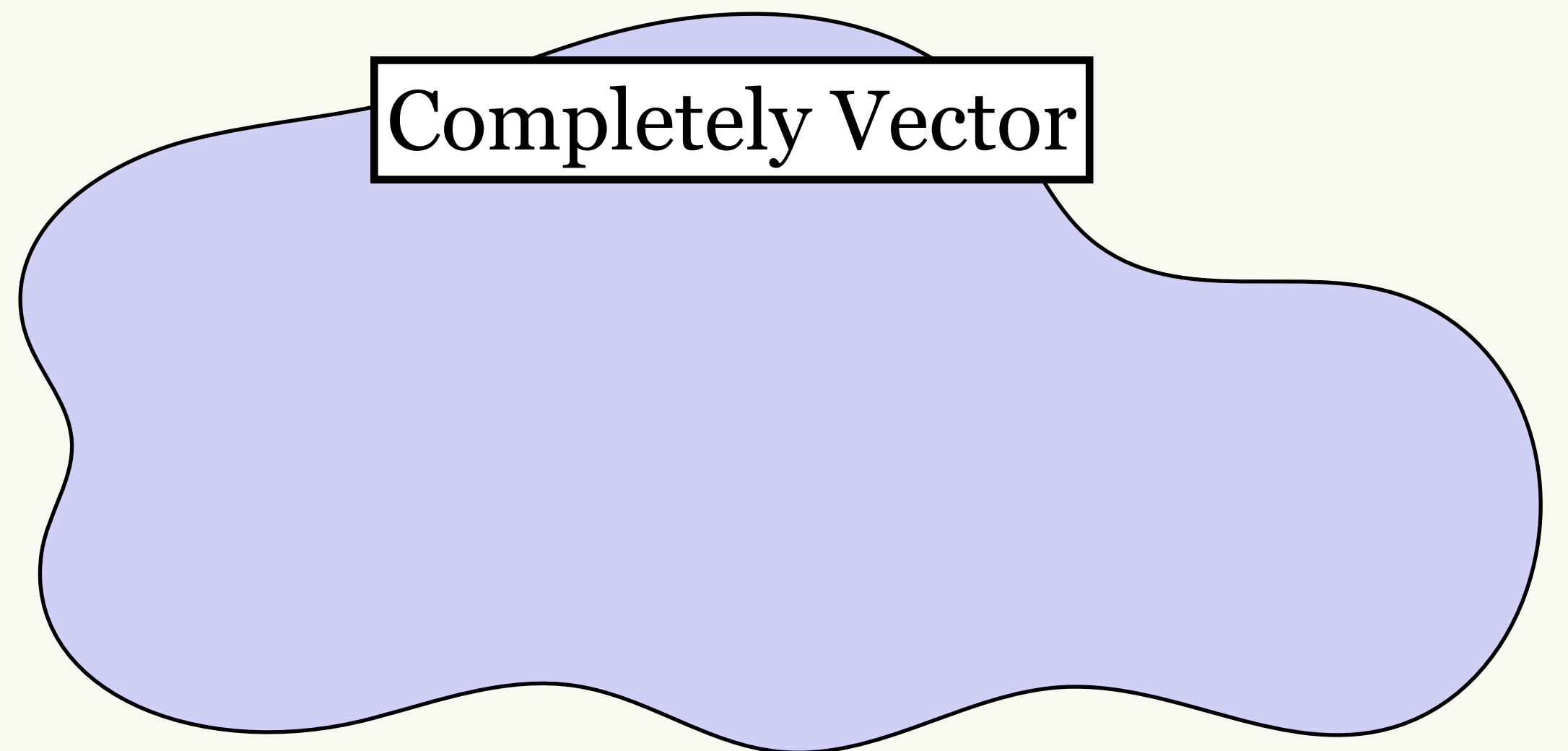
Equality Saturation Compiler

```
(let x (+ a b)
  (let y (+ c d) => (VecAdd
                    (Vec a c)
                    (Vec b d)))
  (Vec x y)))
```

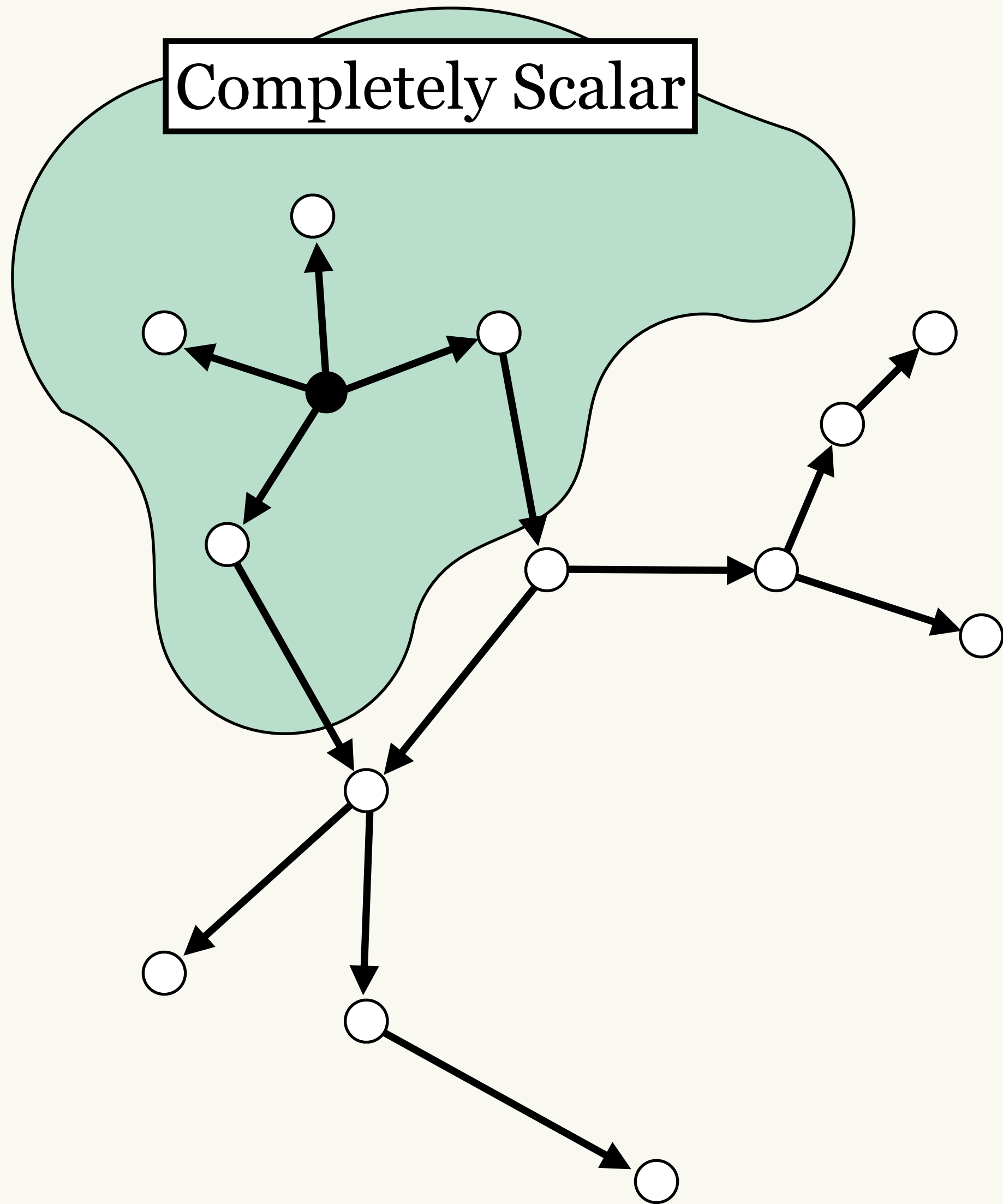
```
(+ a 0) => a
```

```
(VecAdd
 (VecMul a b) => (VecMAC a b c)
 c)
```

Completely Vector



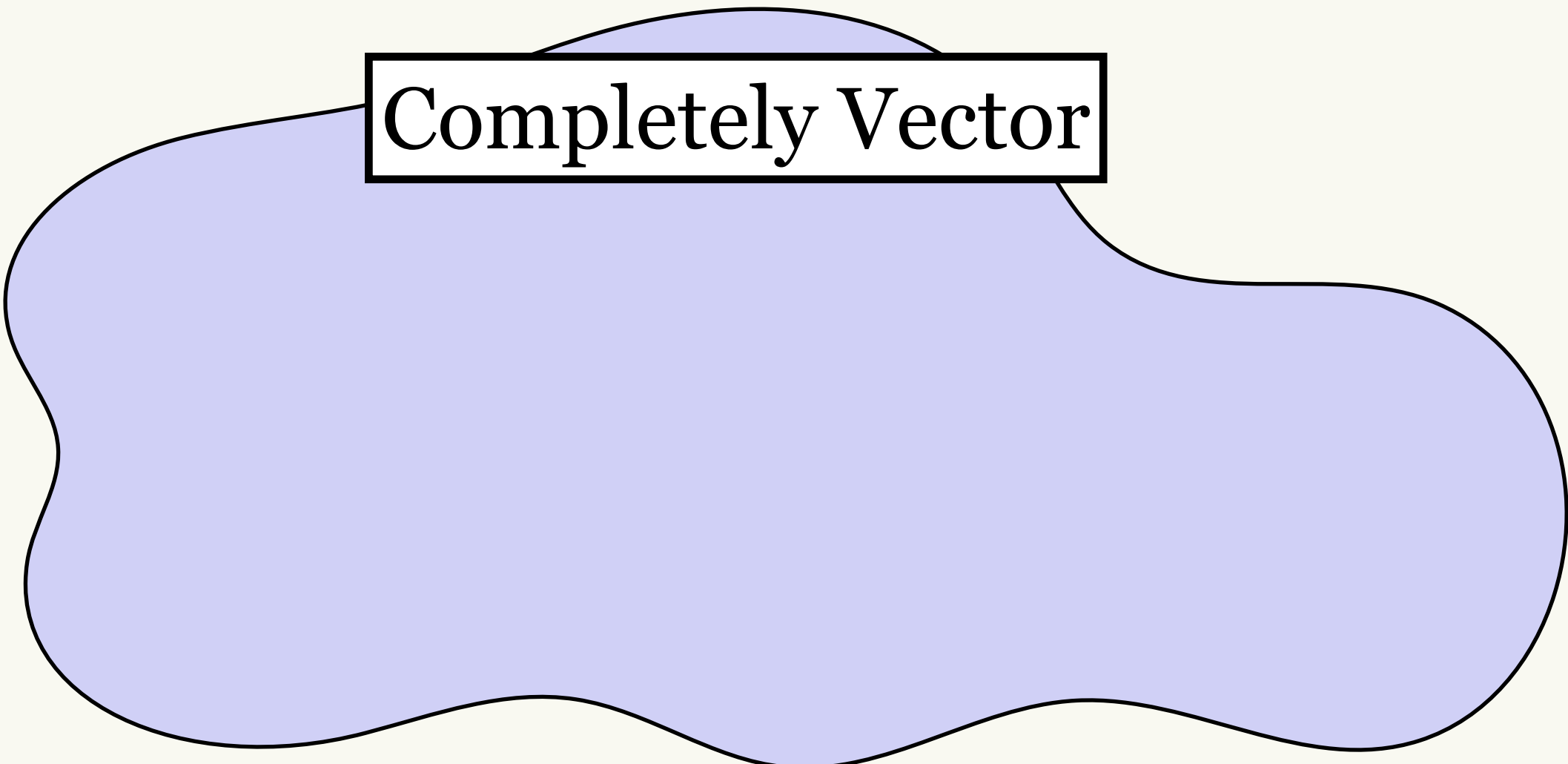
Equality Saturation Compiler



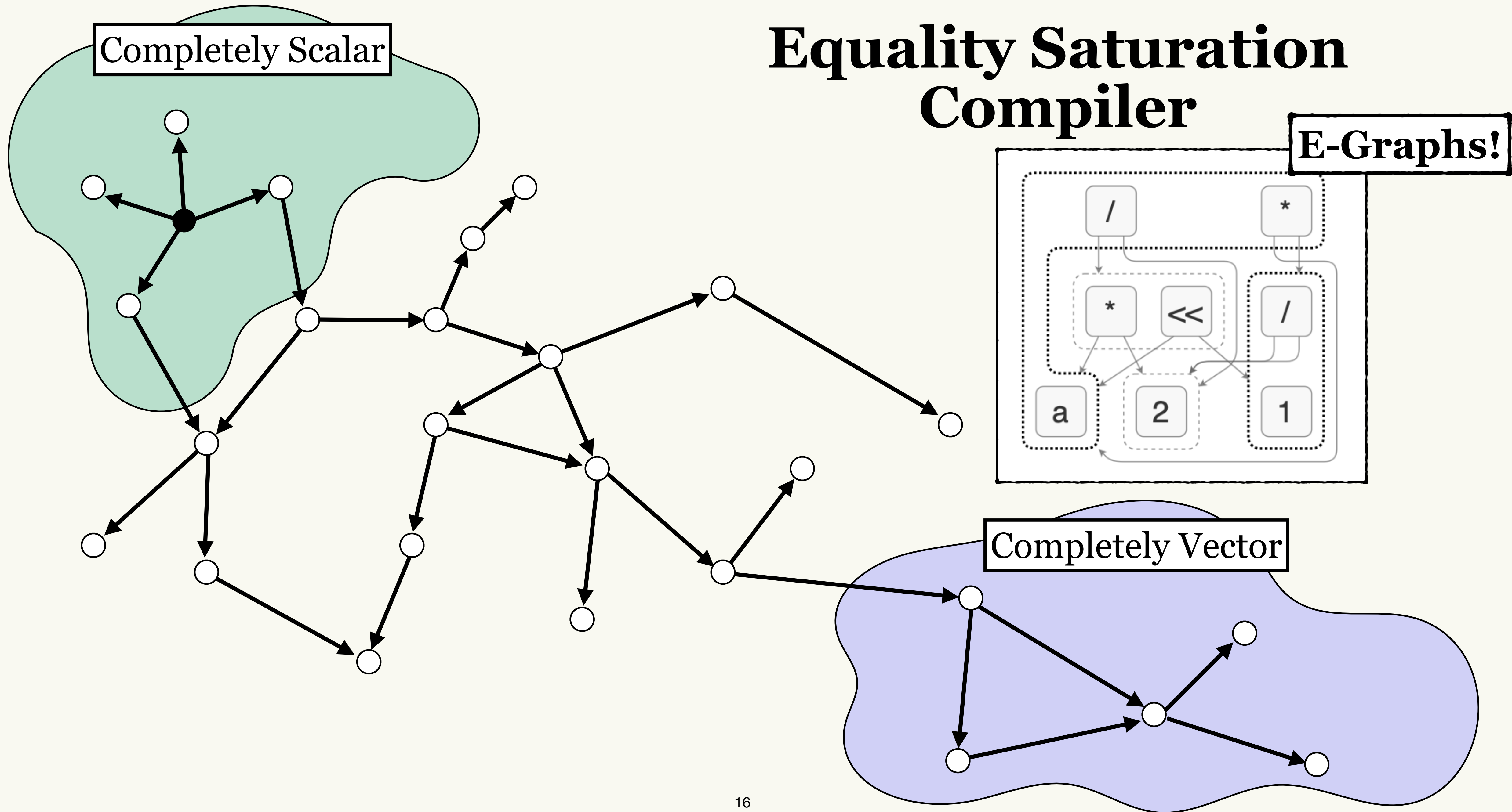
```
(let x (+ a b)
  (let y (+ c d) => (VecAdd
                    (Vec a c)
                    (Vec b d))))
```

```
(+ a 0) => a
```

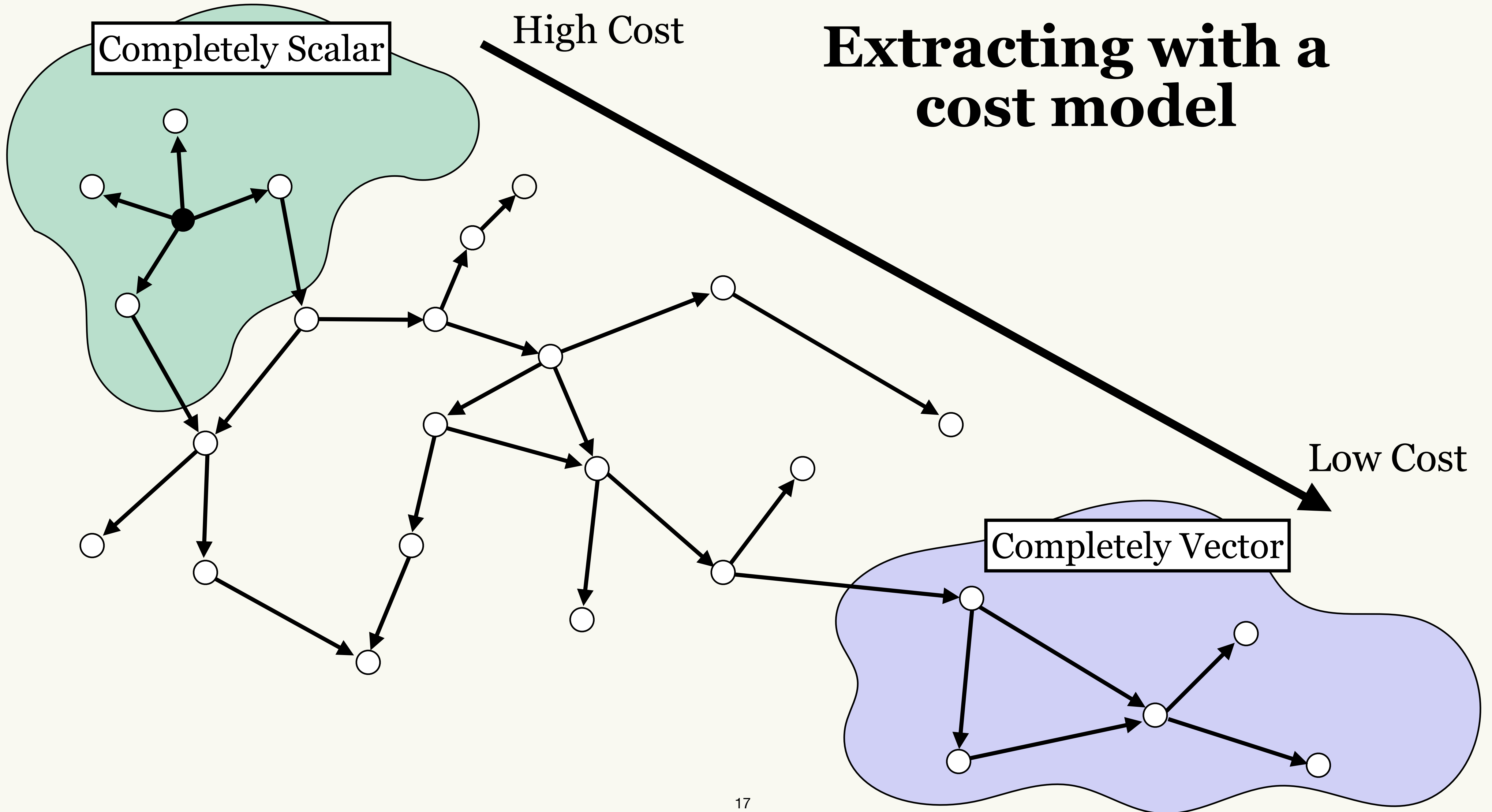
```
(VecAdd
  (VecMul a b) => (VecMAC a b c)
  c)
```



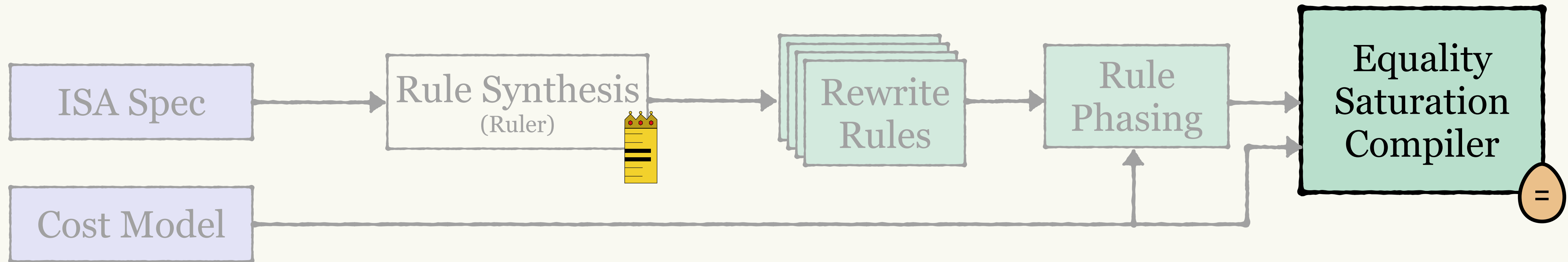
Equality Saturation Compiler



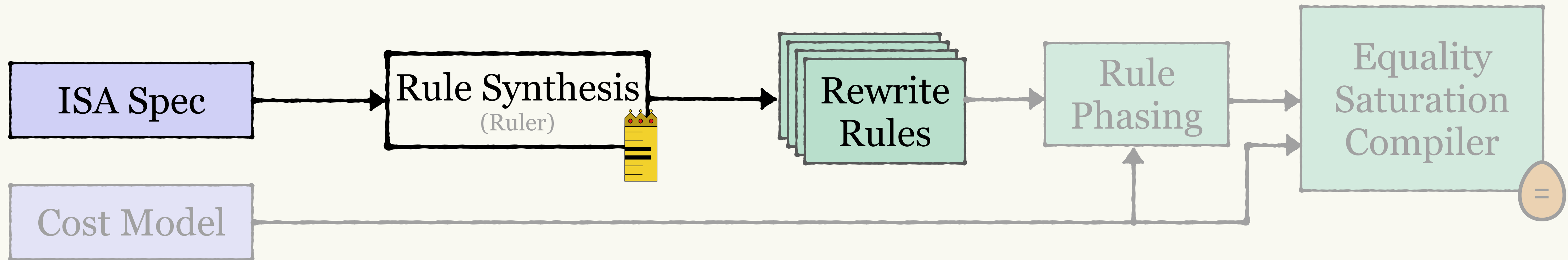
Extracting with a cost model



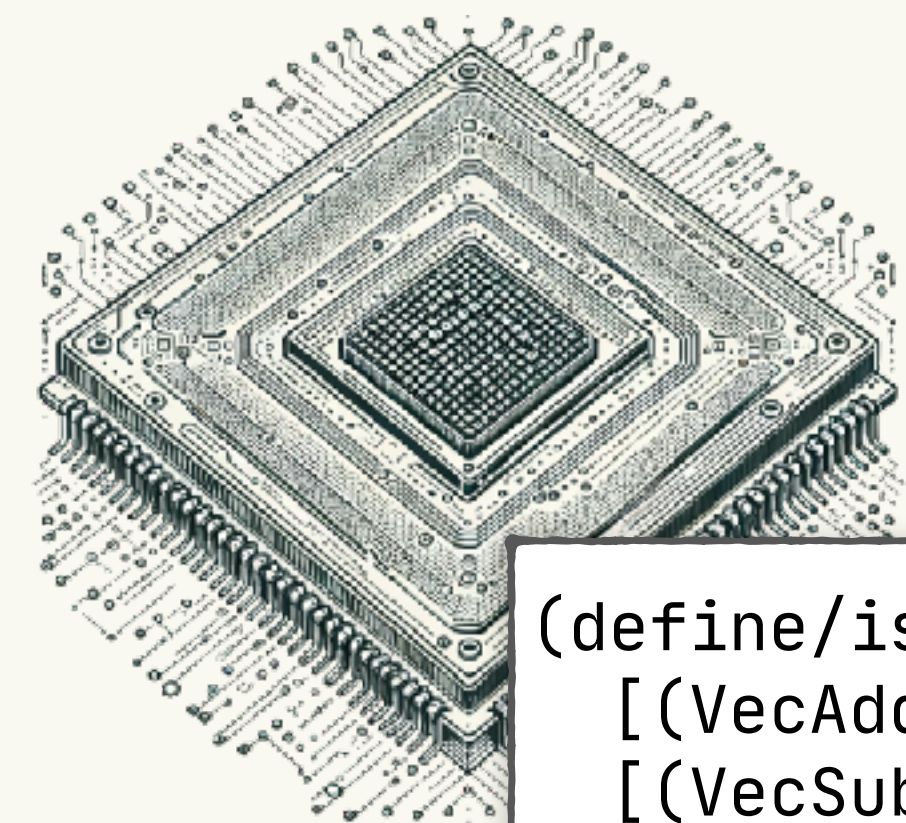
Isaria



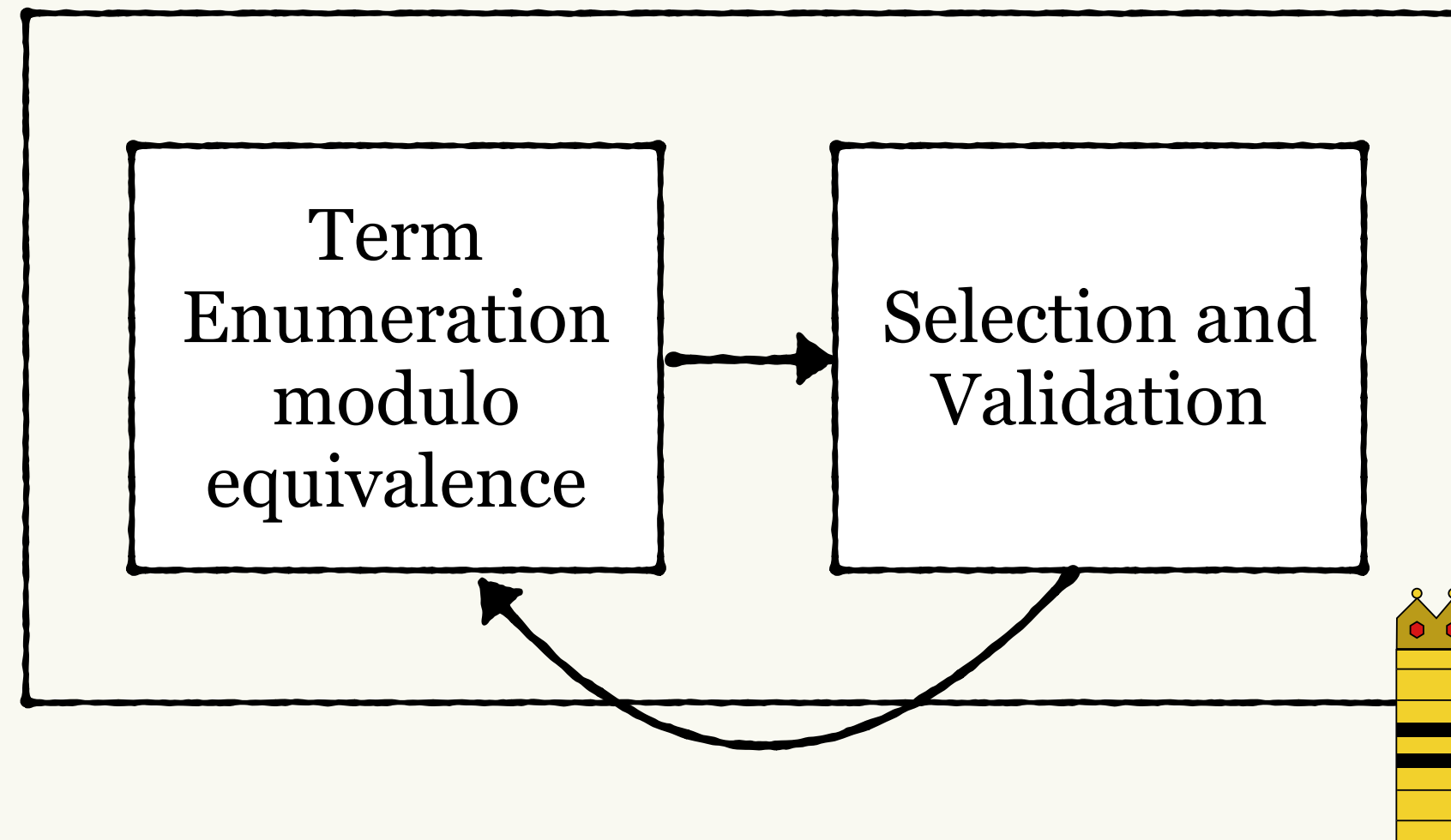
Isaria



Generating Rewrite Rules



```
(define/isa
 [(VecAdd x y) ..]
 [(VecSub x y) ..]
 [(+ x y) ..]
 ..)
```



Rewrite Rules

$(\text{Vec } (+ \text{ ?a } \text{ ?b})) \iff (\text{VecAdd } (\text{Vec } \text{ ?a}) (\text{Vec } \text{ ?b}))$

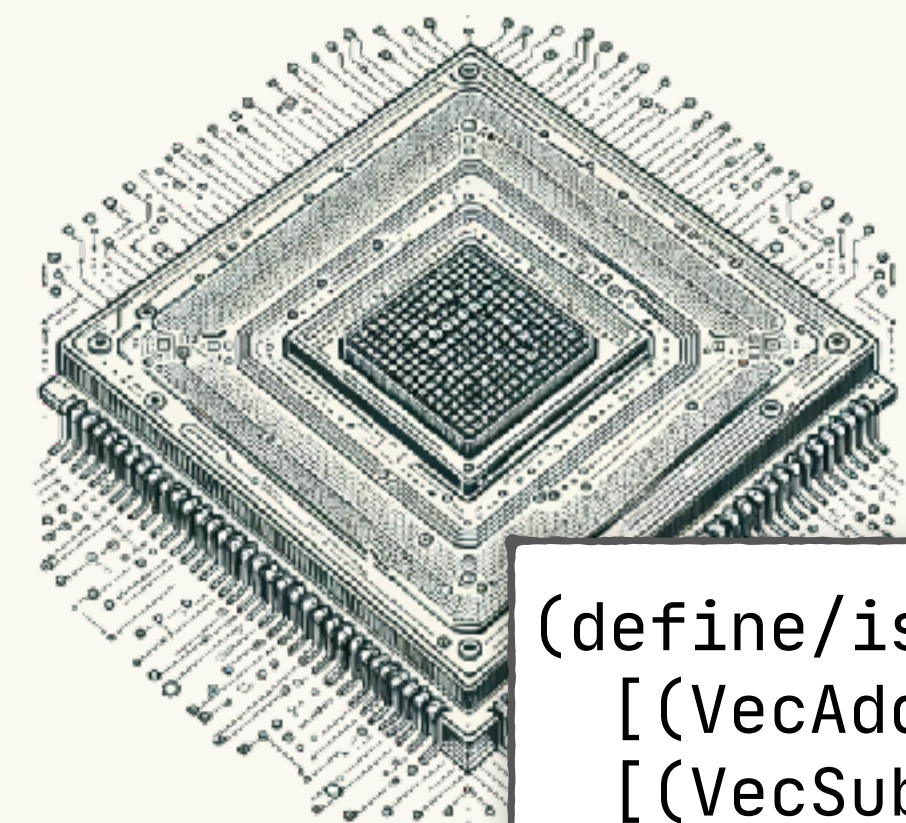
$(\text{Vec } (* \text{ ?a } \text{ ?b})) \iff (\text{VecMul } (\text{Vec } \text{ ?a}) (\text{Vec } \text{ ?b}))$

$(+ \text{ ?a } \text{ ?b}) \iff (+ \text{ ?b } \text{ ?a})$

$(* \text{ ?a } \text{ ?b}) \iff (* \text{ ?b } \text{ ?a})$

⋮

Too many rules...



```
(define/isa
 [(VecAdd x y) ..]
 [(VecSub x y) ..]
 [(+ x y) ..]
 ..)
```

Term
Enumeration
modulo
equivalence

Selection and
Validation

Rewrite Rules

$(\text{Vec } (+ \text{ ?a } \text{ ?b})) \iff (\text{VecAdd } (\text{Vec } \text{ ?a}) (\text{Vec } \text{ ?b}))$

$(\text{Vec } (* \text{ ?a } \text{ ?b})) \iff (\text{VecMul } (\text{Vec } \text{ ?a}) (\text{Vec } \text{ ?b}))$

$(+ \text{ ?a } \text{ ?b}) \iff (+ \text{ ?b } \text{ ?a})$

$(* \text{ ?a } \text{ ?b}) \iff (* \text{ ?b } \text{ ?a})$

$(\text{VecAdd } \text{ ?b } \text{ ?a}) \iff (\text{VecAdd } \text{ ?a } \text{ ?b})$

$(\text{VecMinus } \text{ ?b } (\text{VecNeg } \text{ ?a})) \iff (\text{VecAdd } \text{ ?a } \text{ ?b})$

$(\text{sgn } \text{ ?a}) \iff (\text{sgn } (\text{sgn } \text{ ?a}))$

$(\text{neg } (* \text{ ?b } \text{ ?a})) \iff (* \text{ ?b } (\text{neg } \text{ ?a}))$

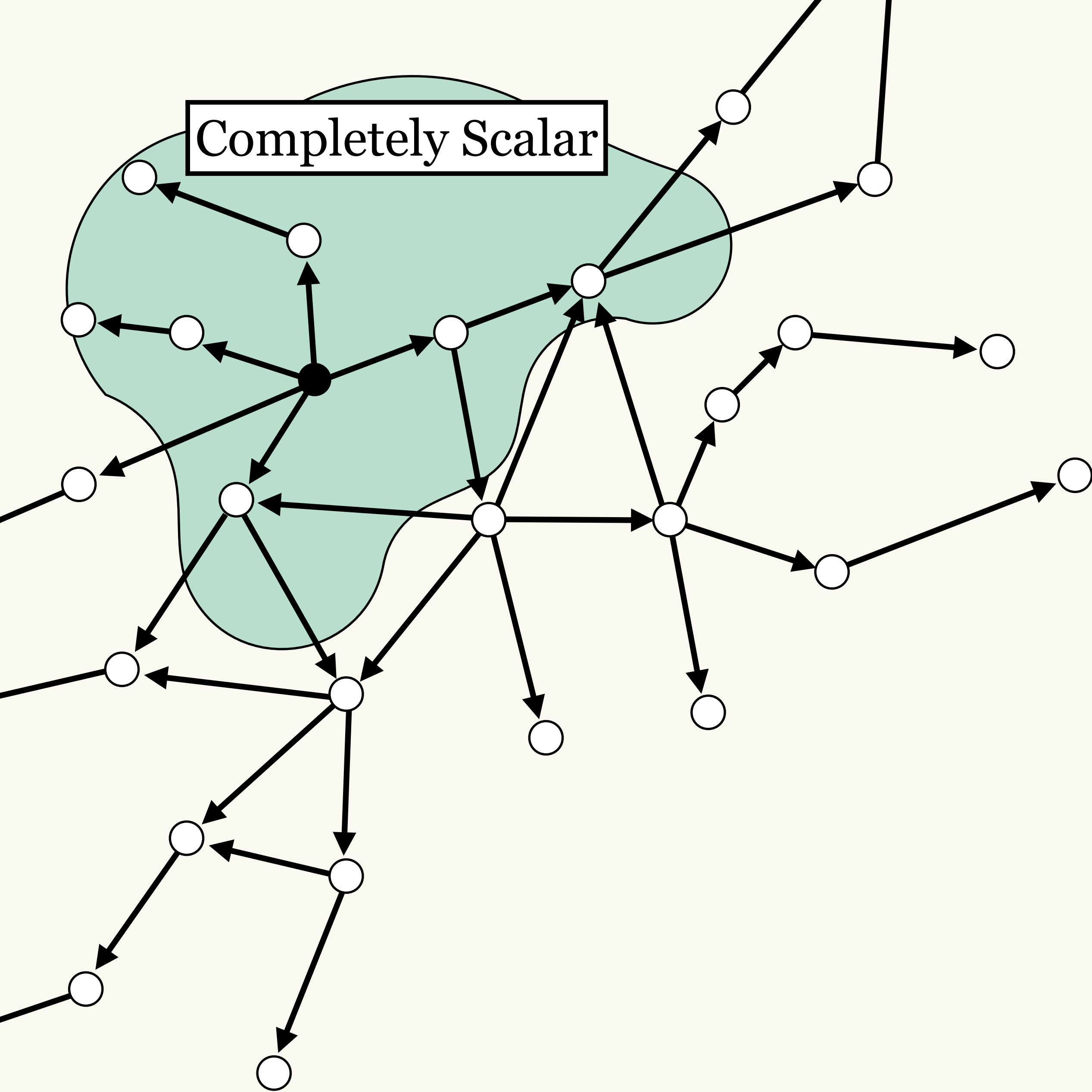
$(\text{VecMAC } \text{ ?c } \text{ ?b } \text{ ?a}) \iff (\text{VecAdd } \text{ ?c } (\text{VecMul } \text{ ?b } \text{ ?a}))$

$(\text{VecMul } \text{ ?b } \text{ ?a}) \iff (\text{VecMul } \text{ ?a } \text{ ?b})$

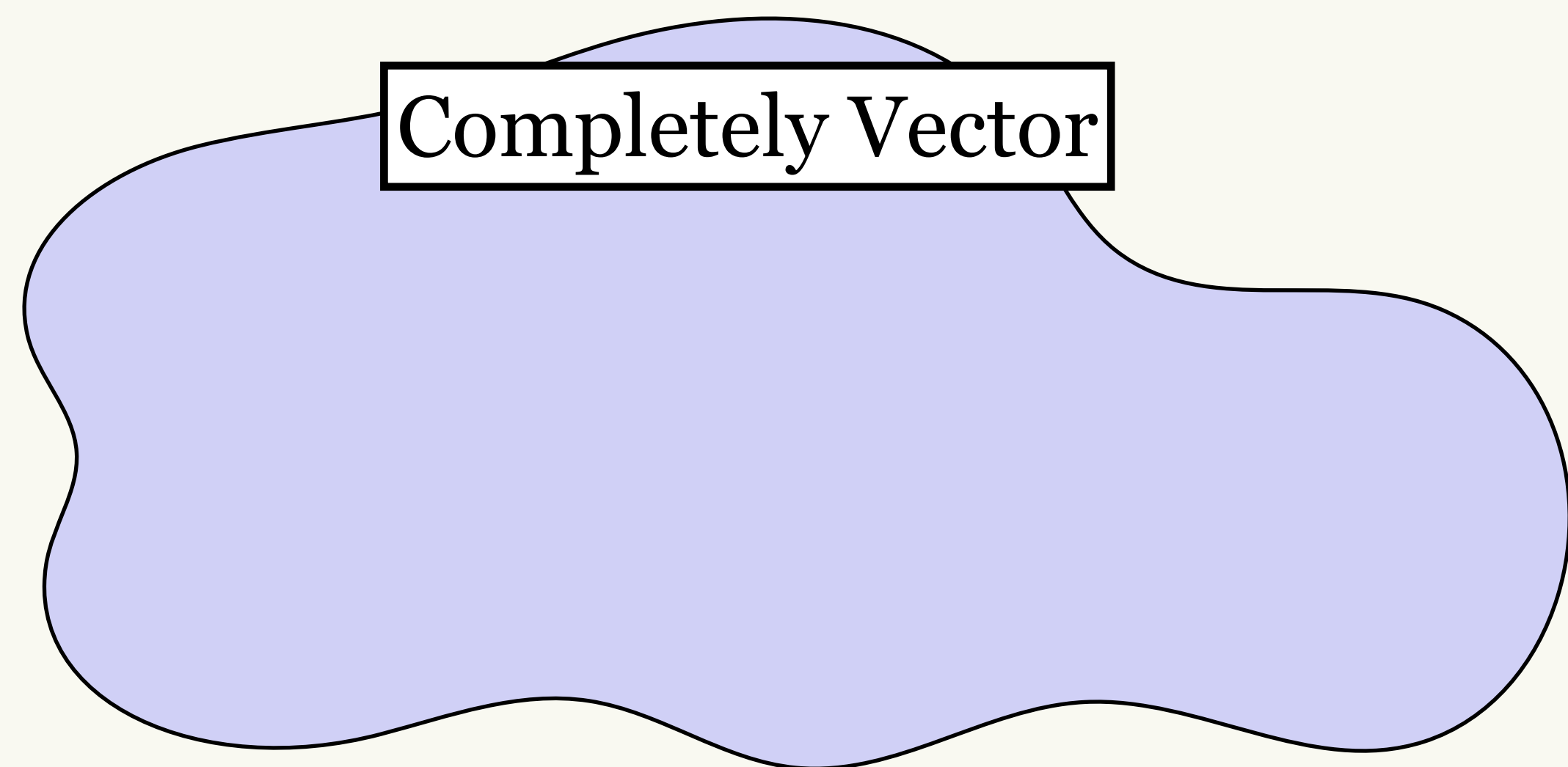
$(/ \text{ ?a } \text{ ?b}) \iff (/ \text{ ?a } (\text{sgn } \text{ ?b}))$

$(\text{VecNeg } (\text{VecMul } \text{ ?b } \text{ ?a})) \iff (\text{VecMul } \text{ ?a } (\text{VecNeg } \text{ ?b}))$

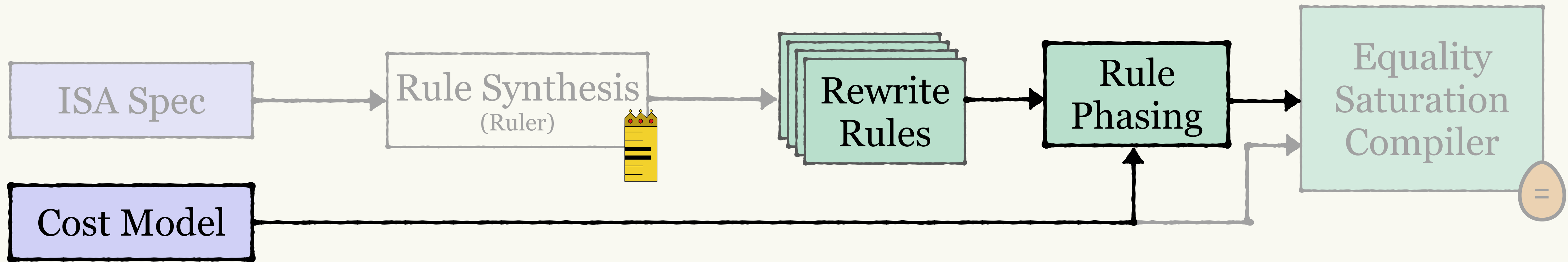
⋮



Too many rules...

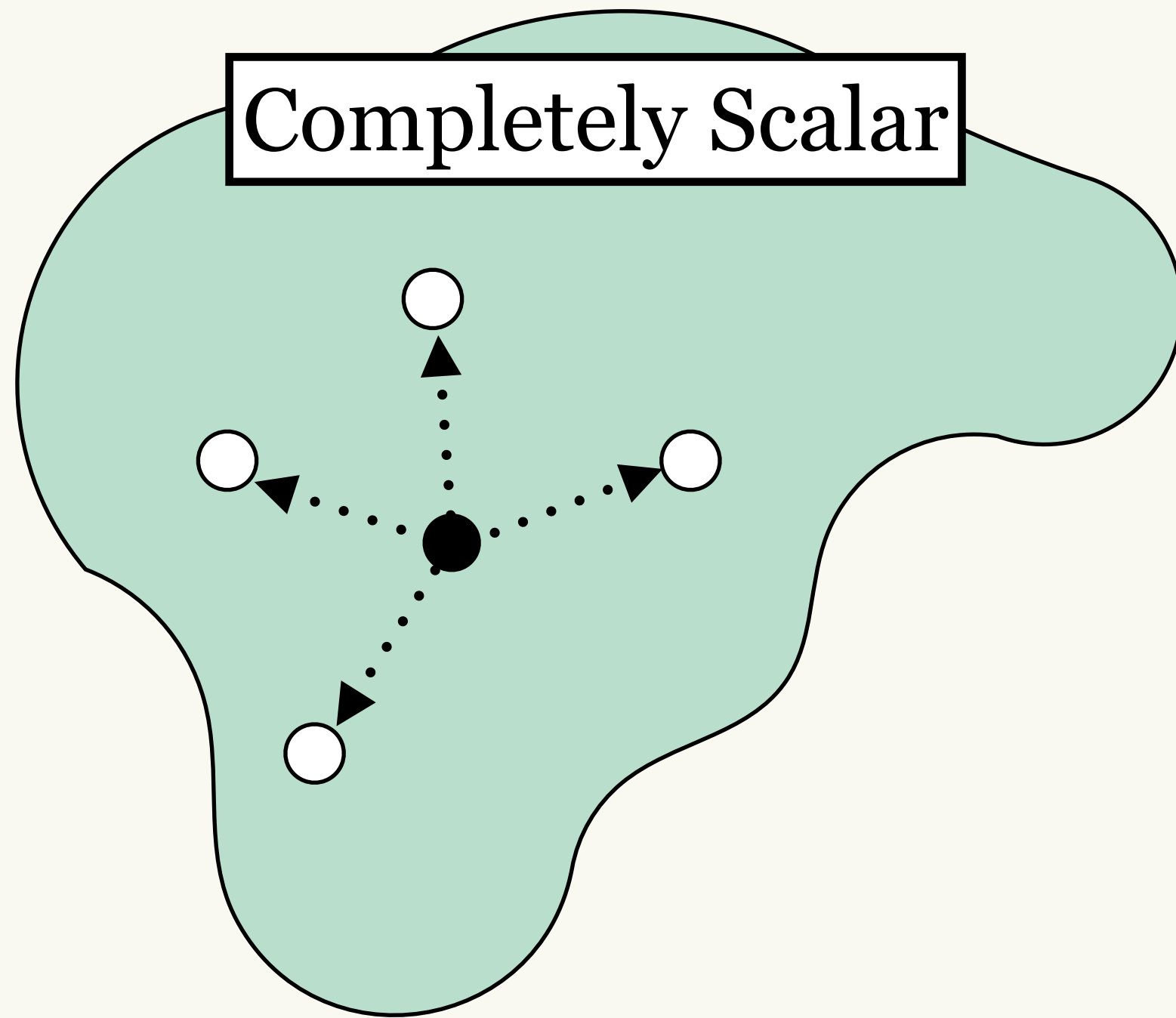


Isaria

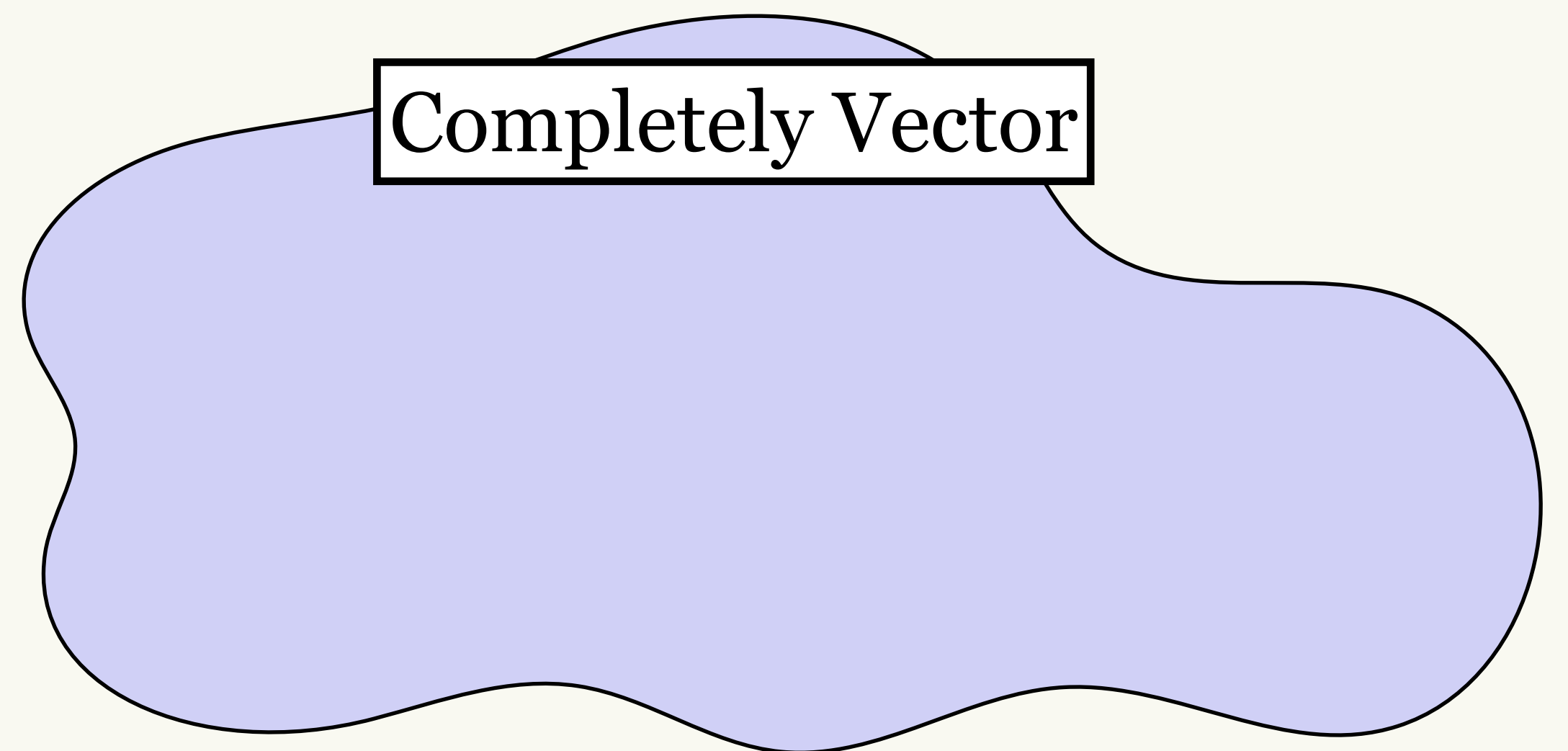


1. Rule Phasing

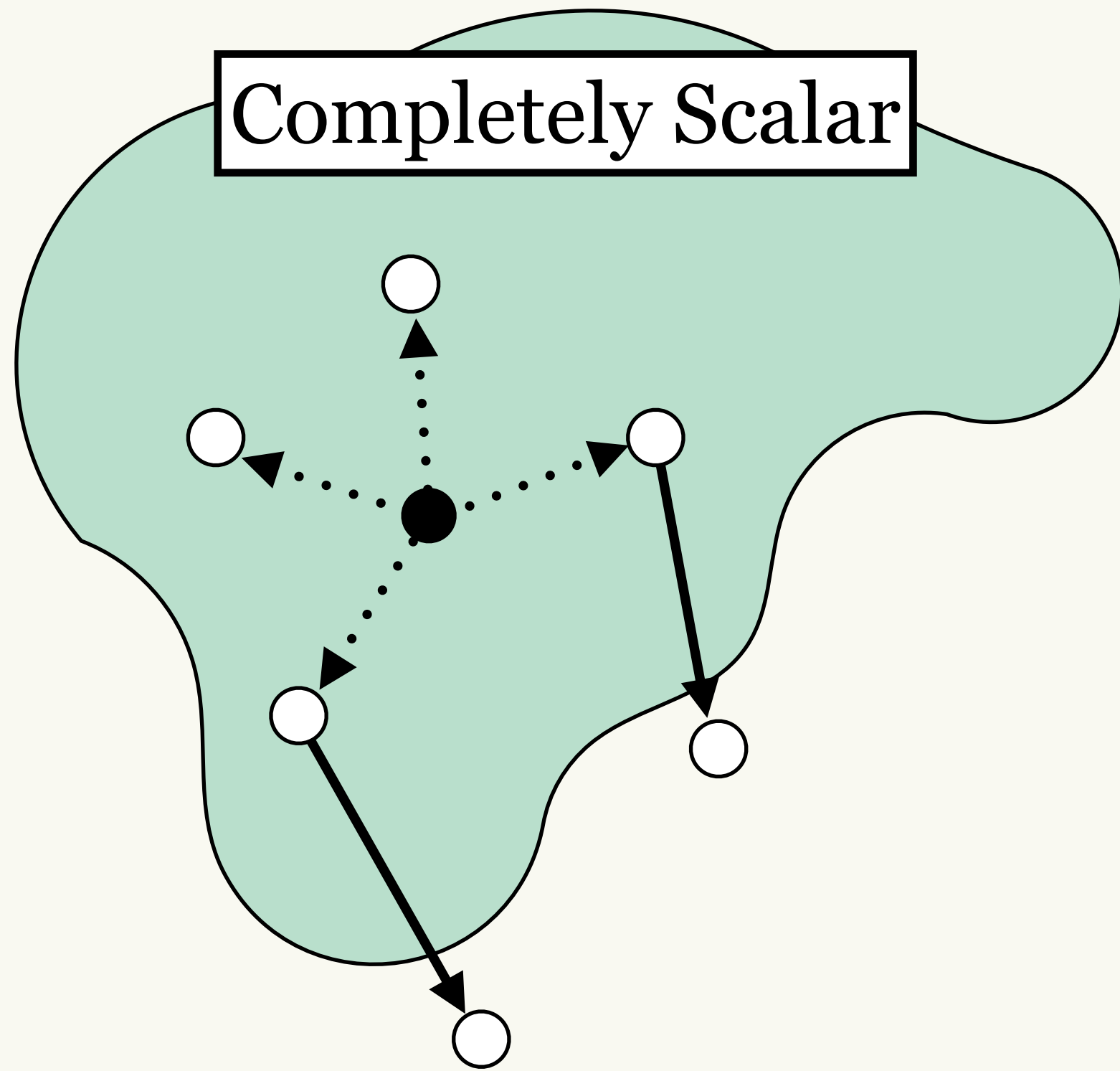
2. Pruning



Expansion



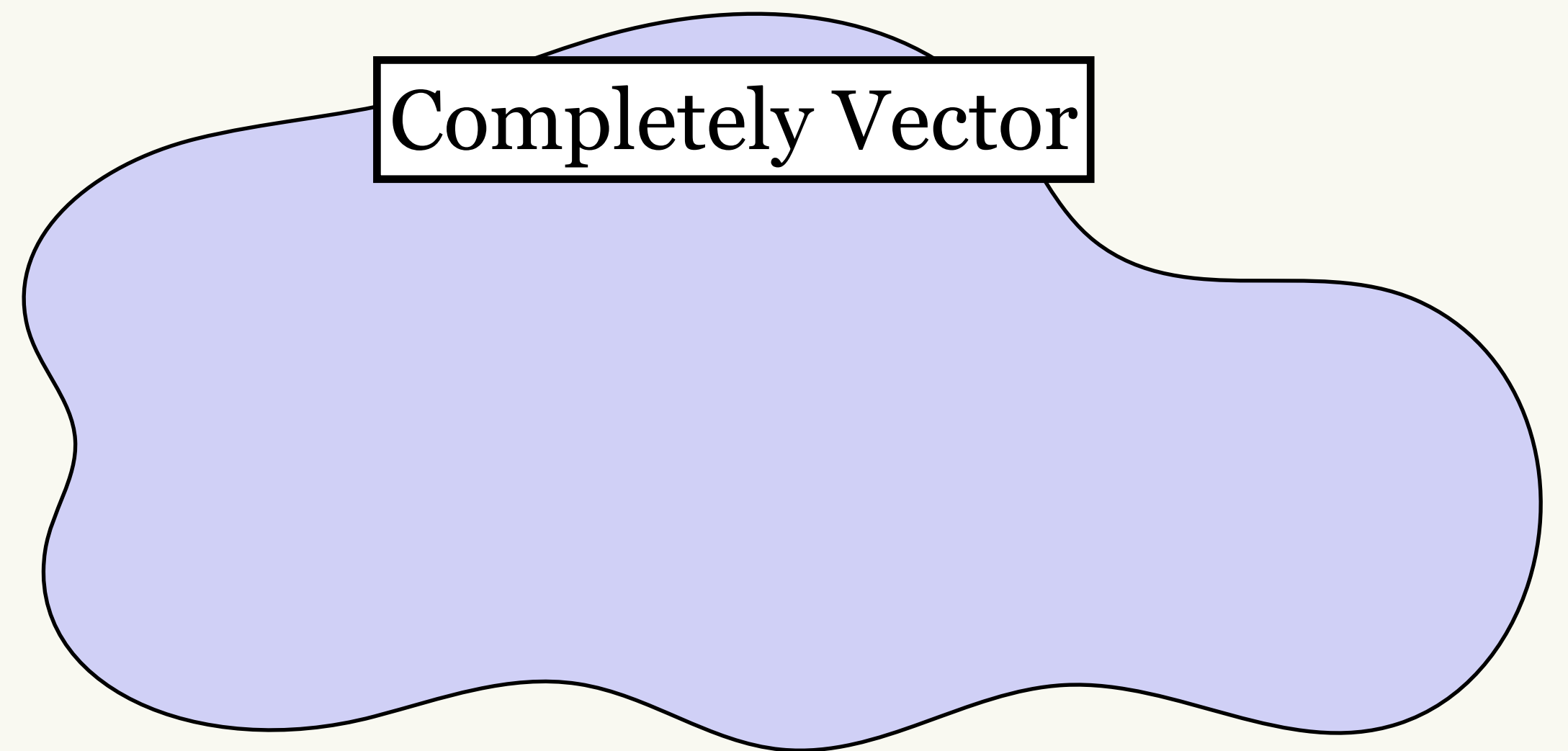
1. Rule Phasing



2. Pruning

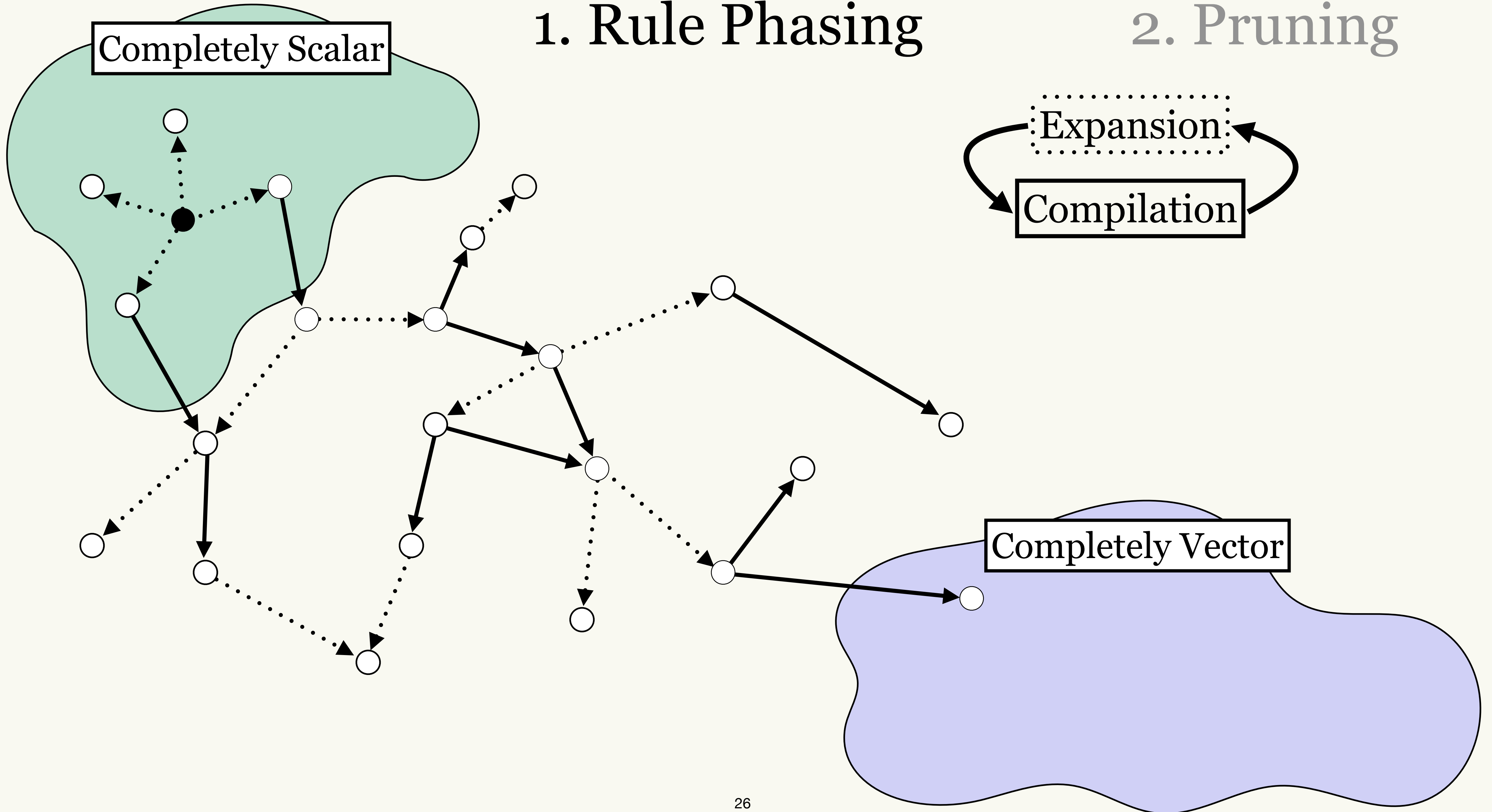
Expansion

Compilation



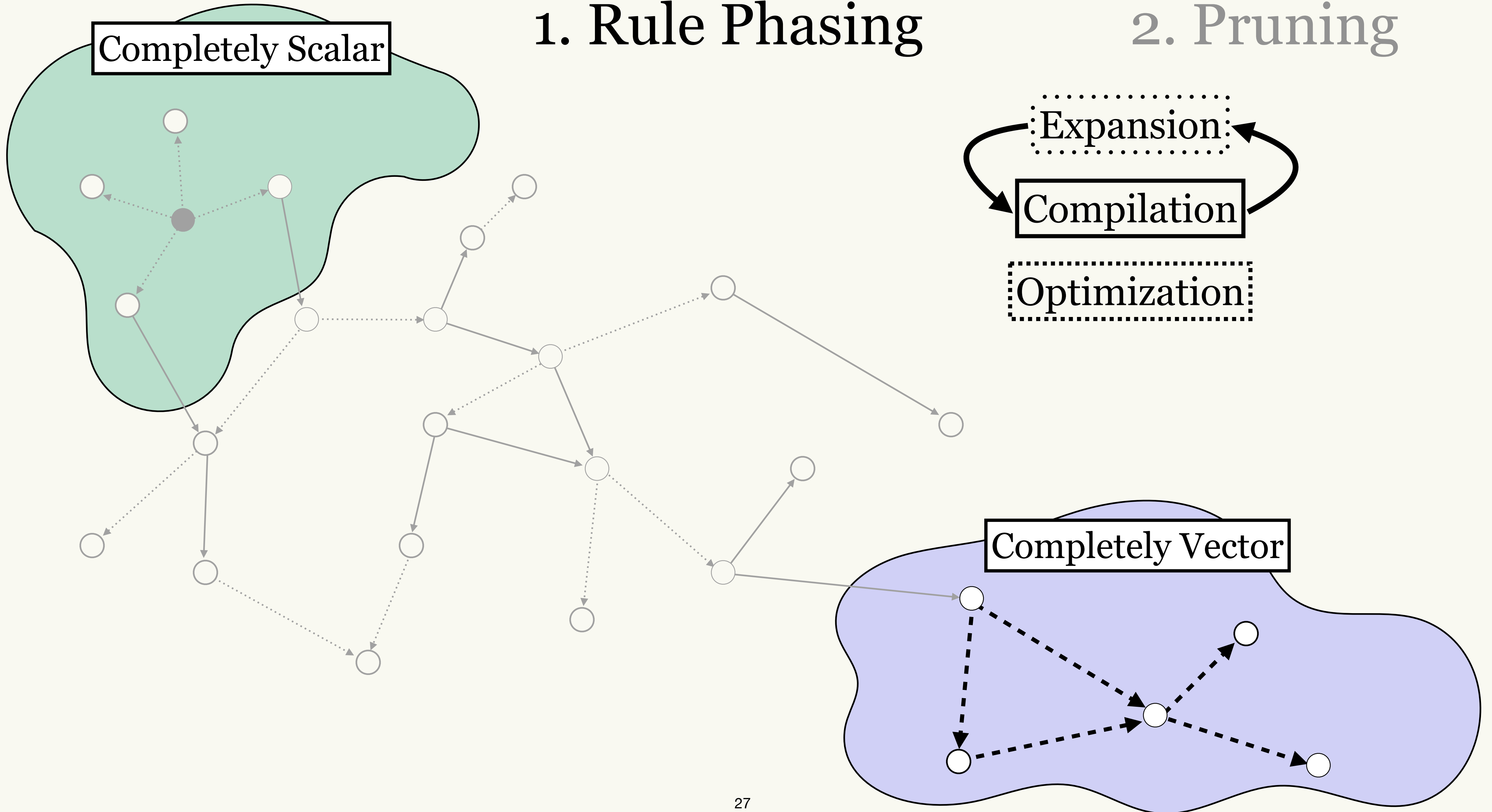
1. Rule Phasing

2. Pruning

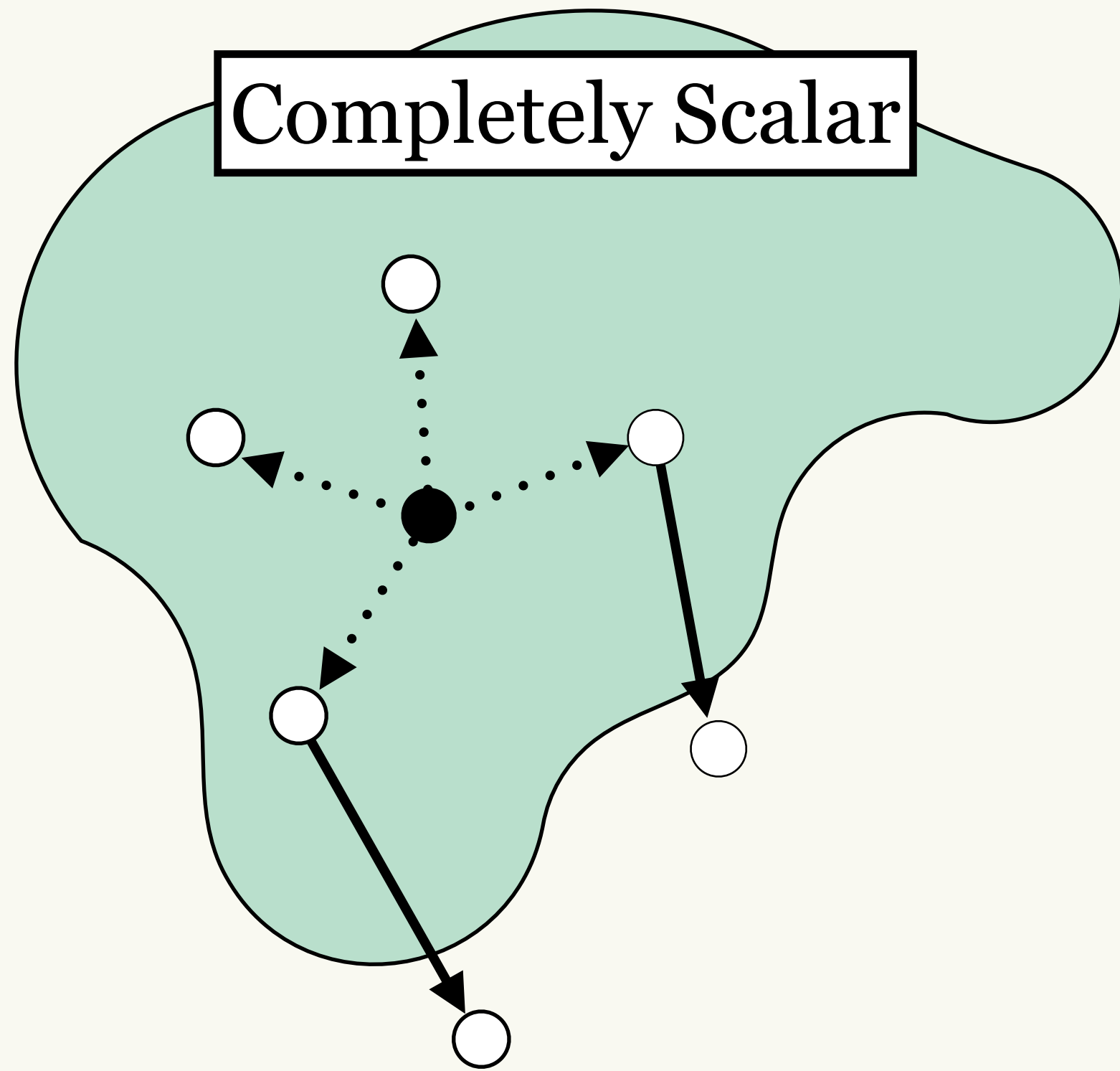


1. Rule Phasing

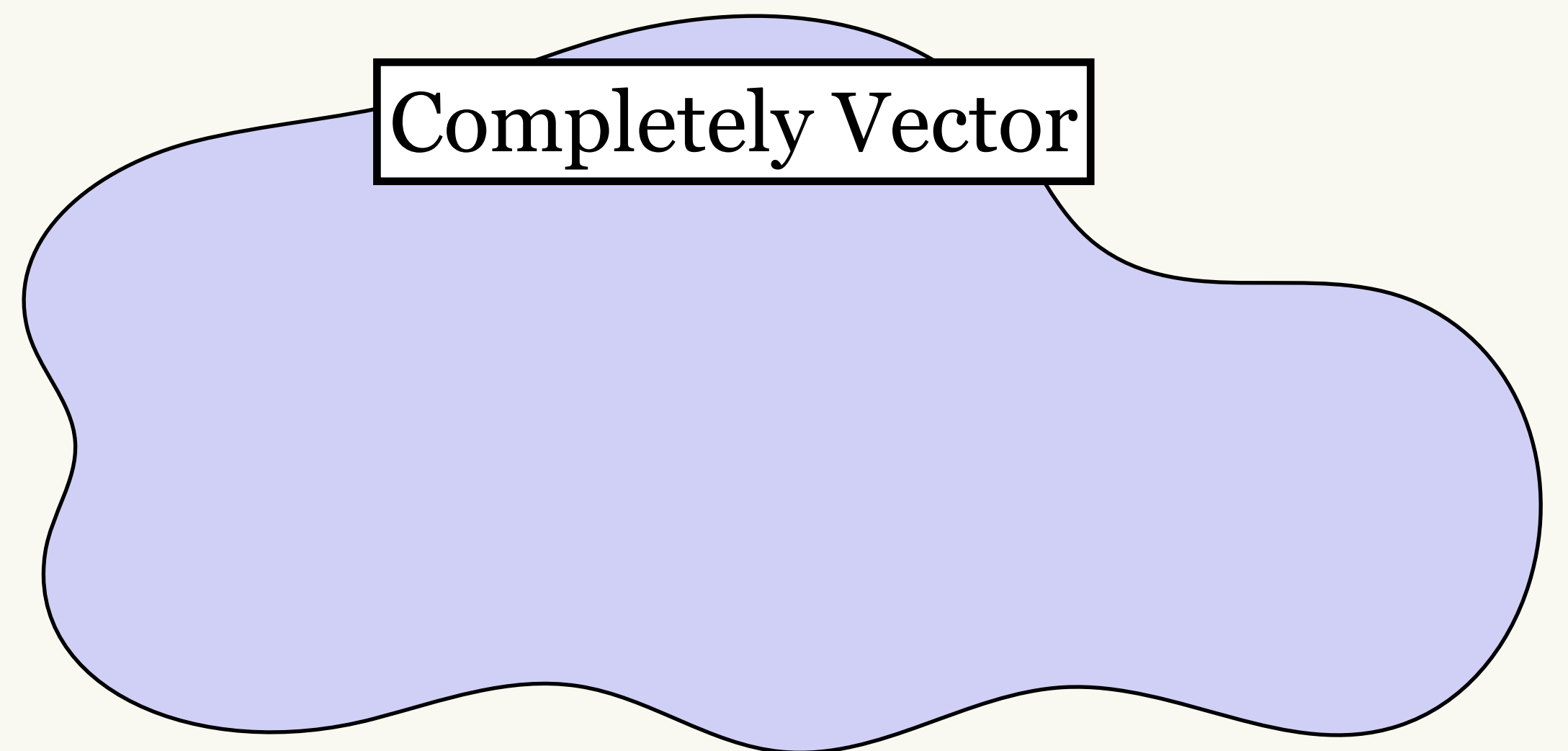
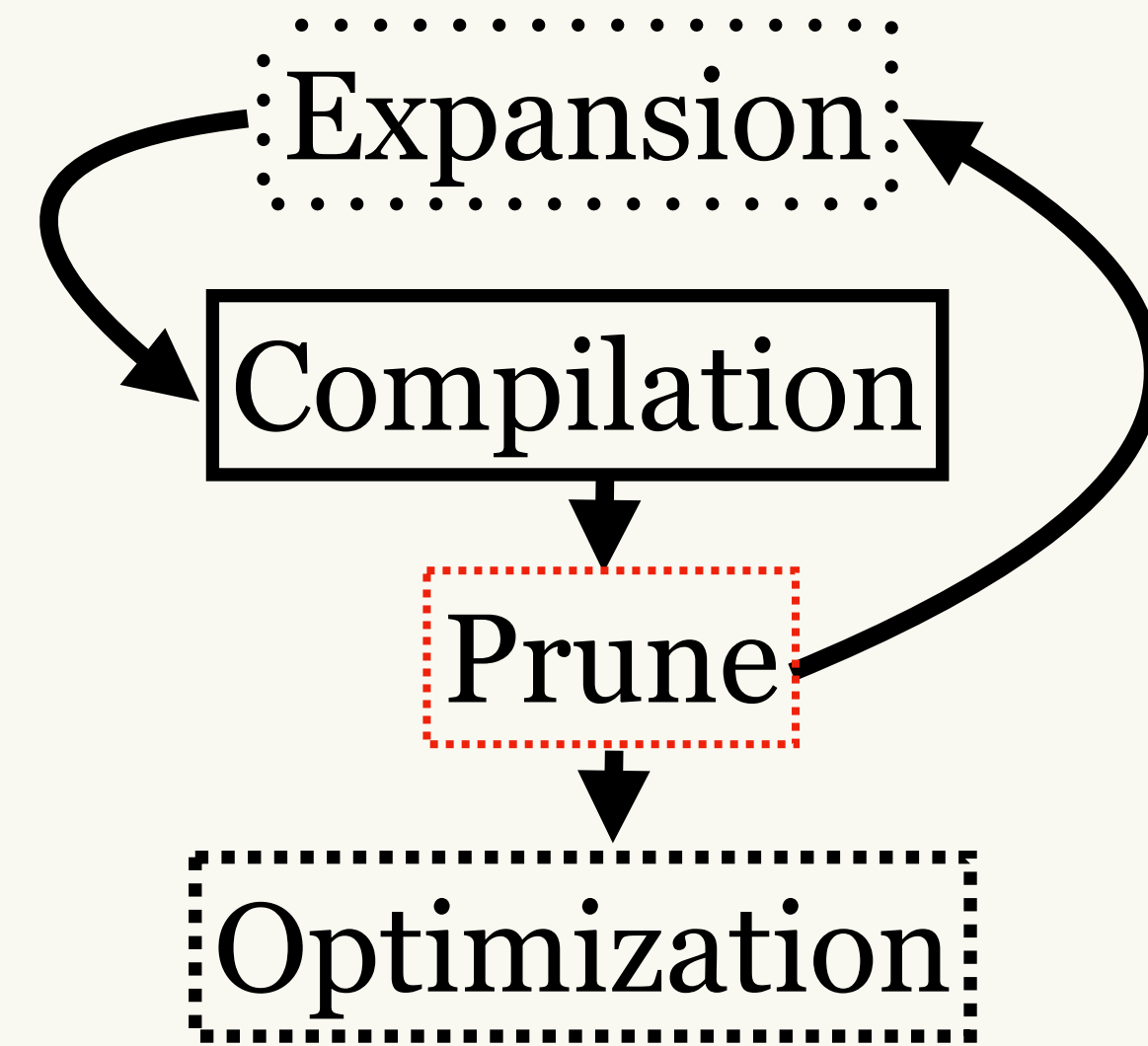
2. Pruning



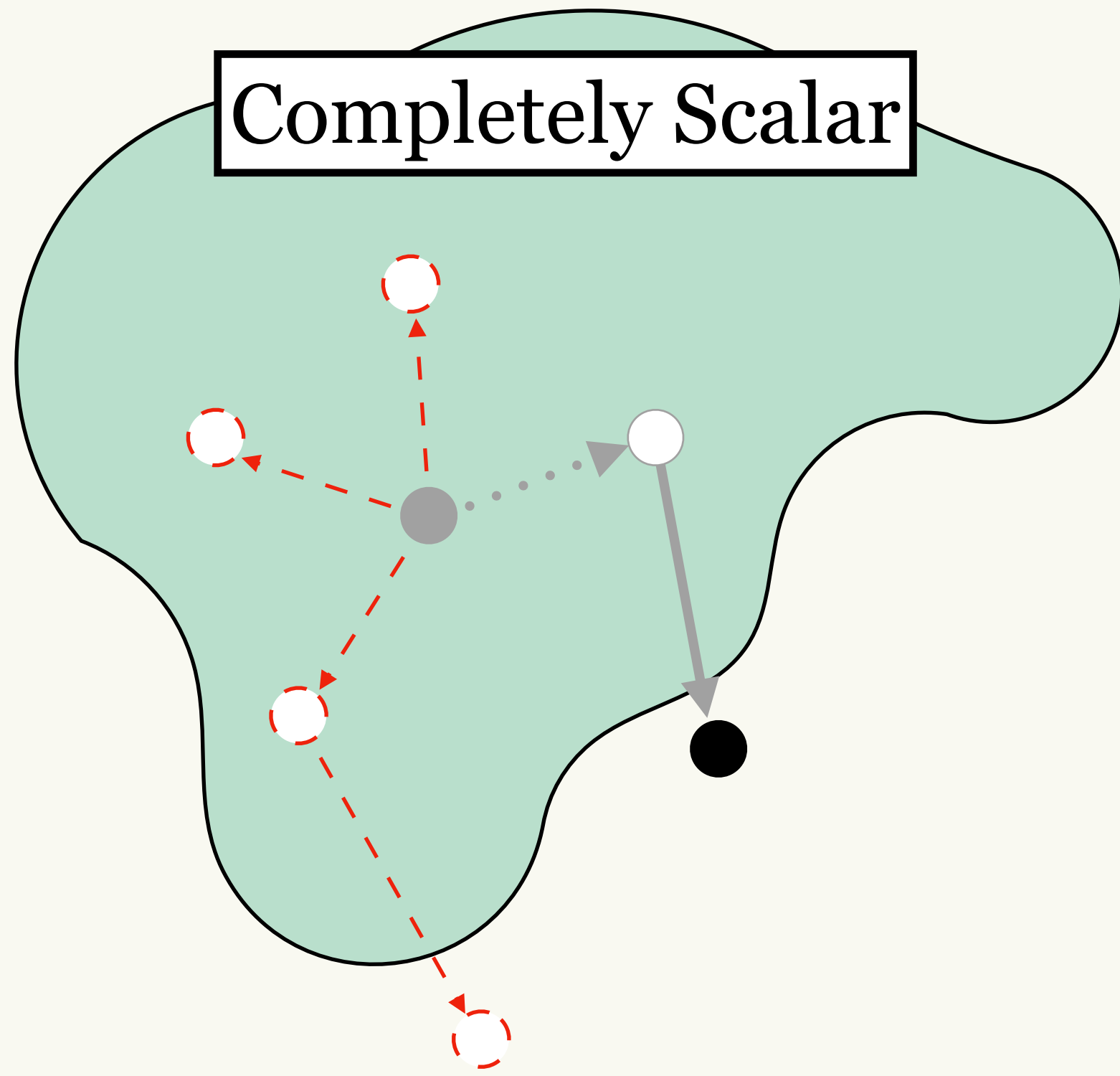
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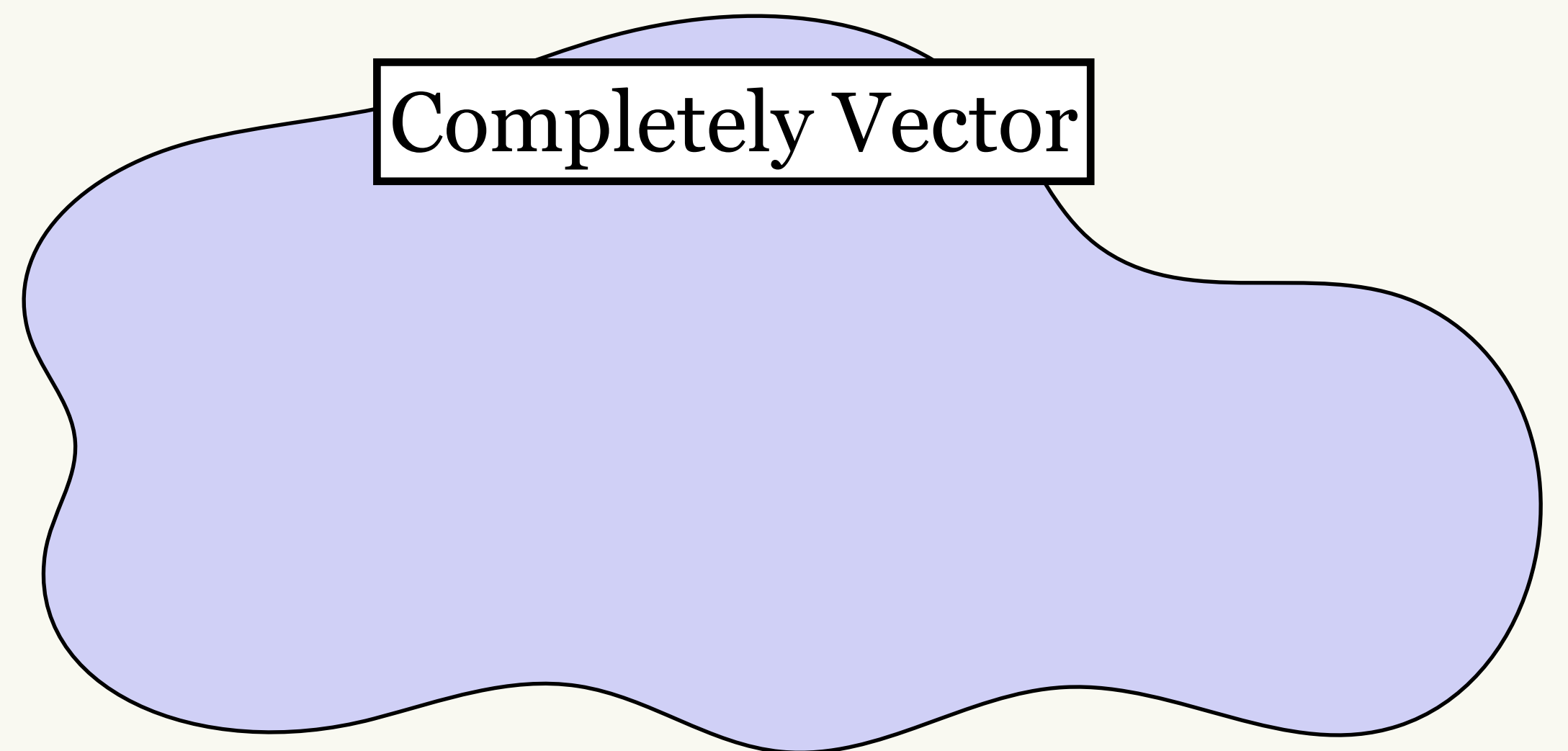
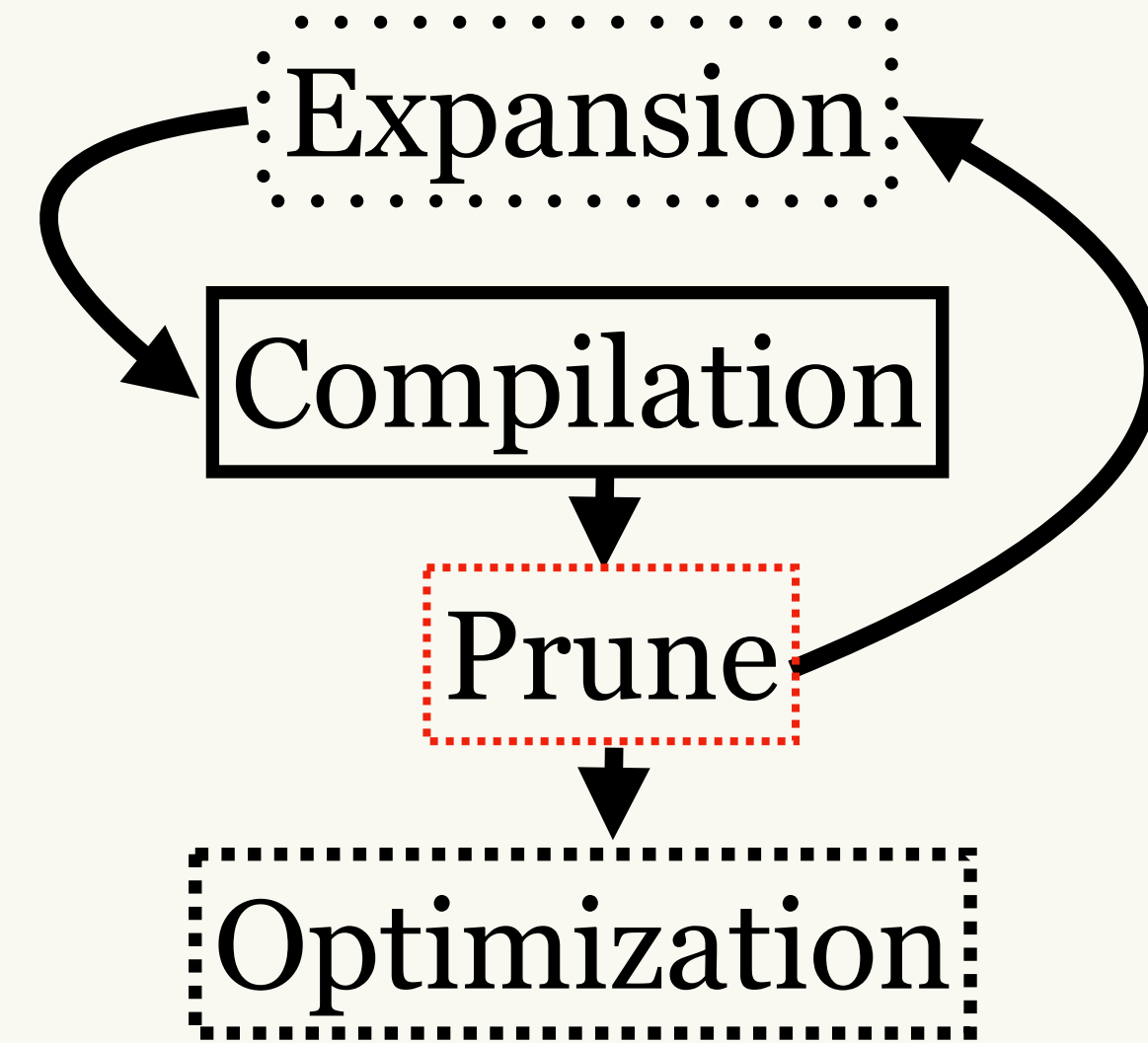
2. Pruning



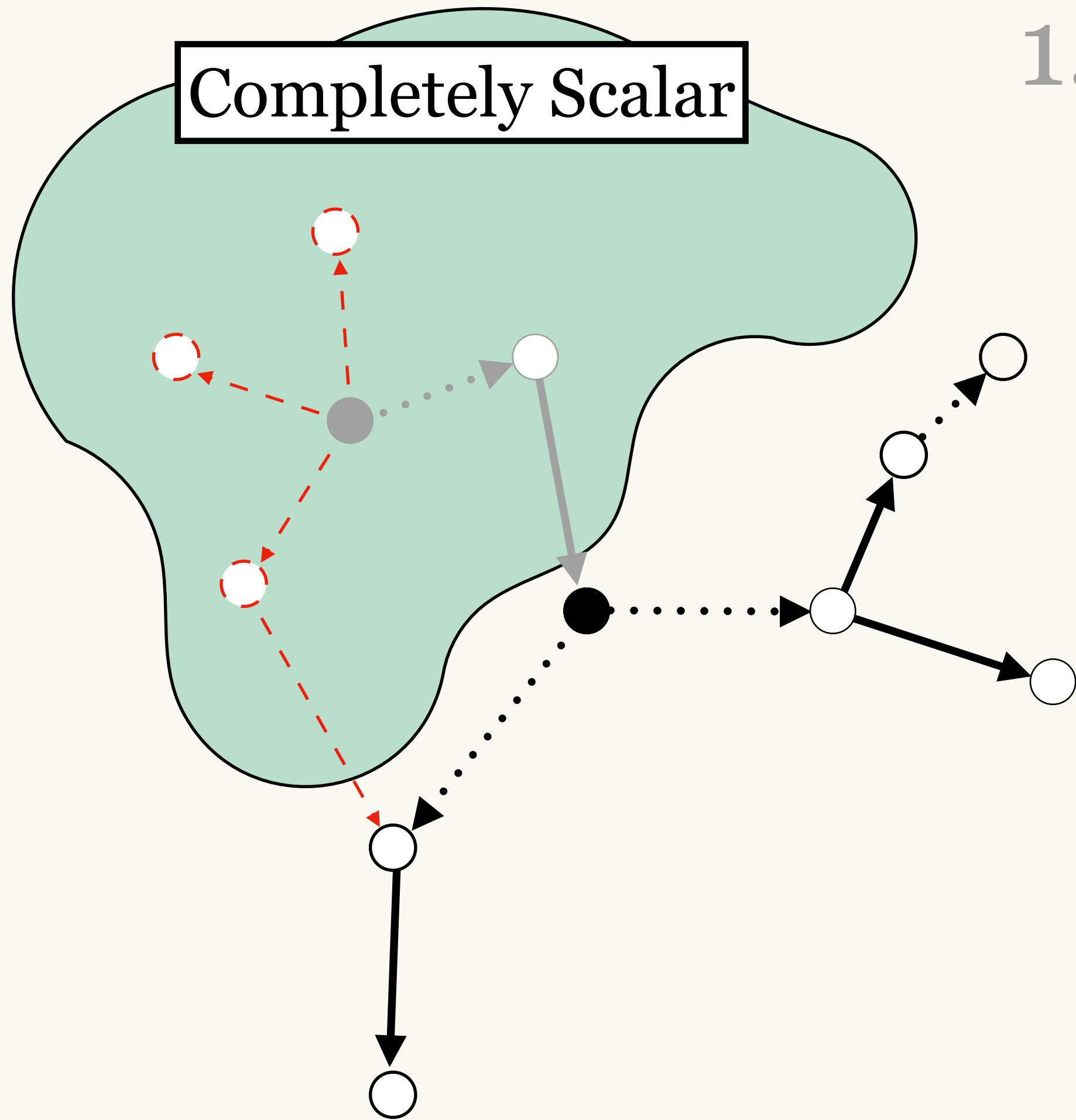
1. Rule Phasing



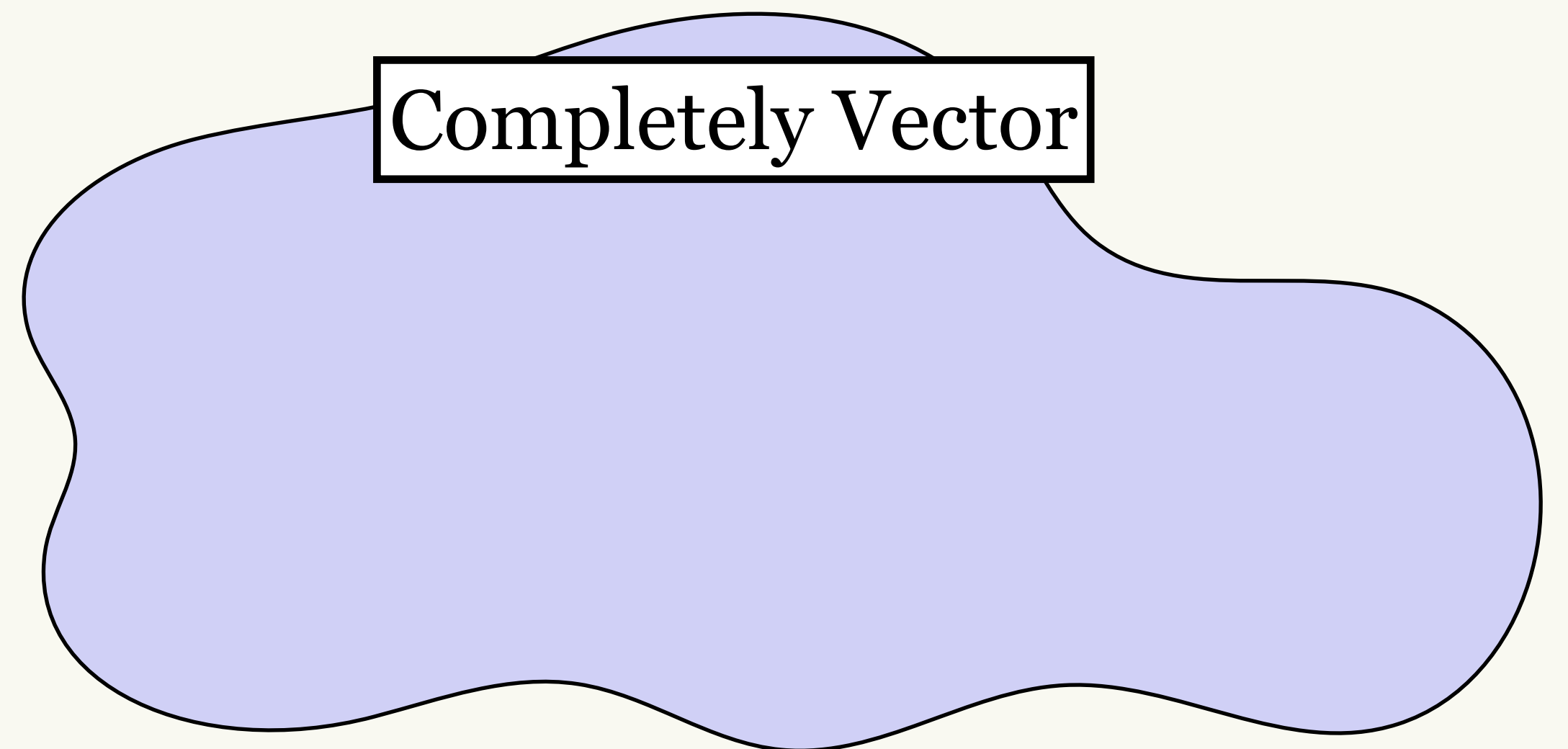
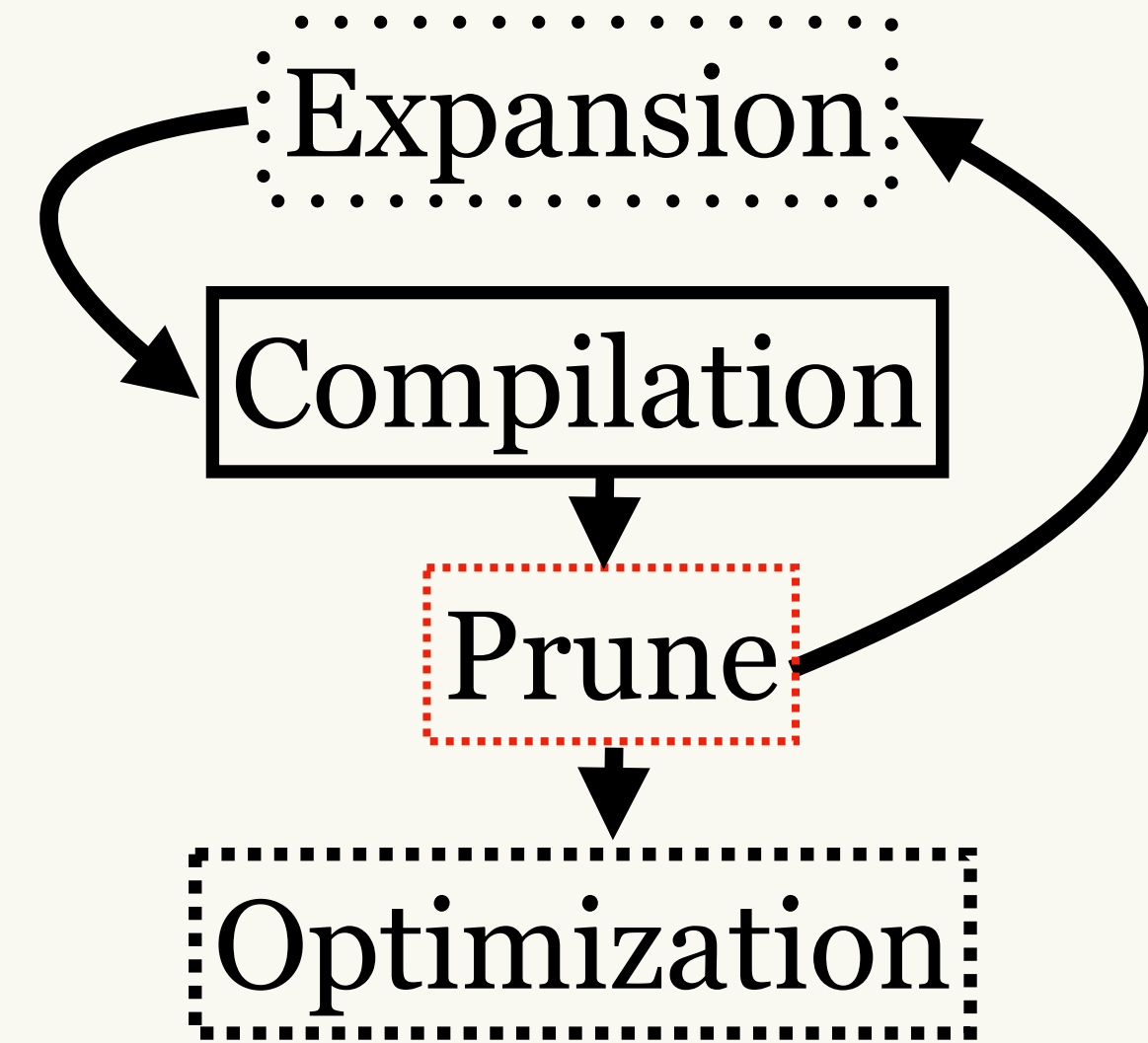
2. Pruning



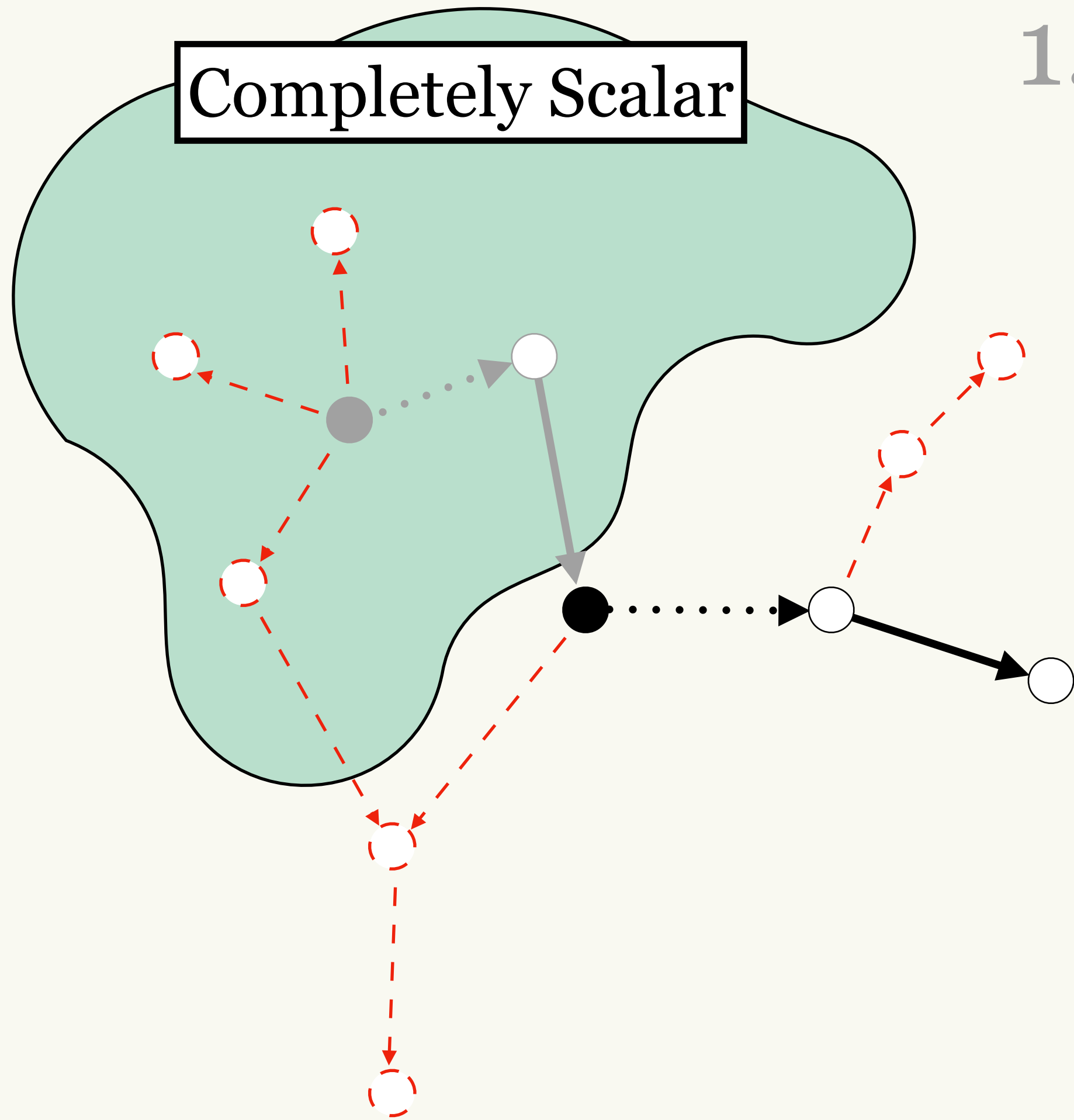
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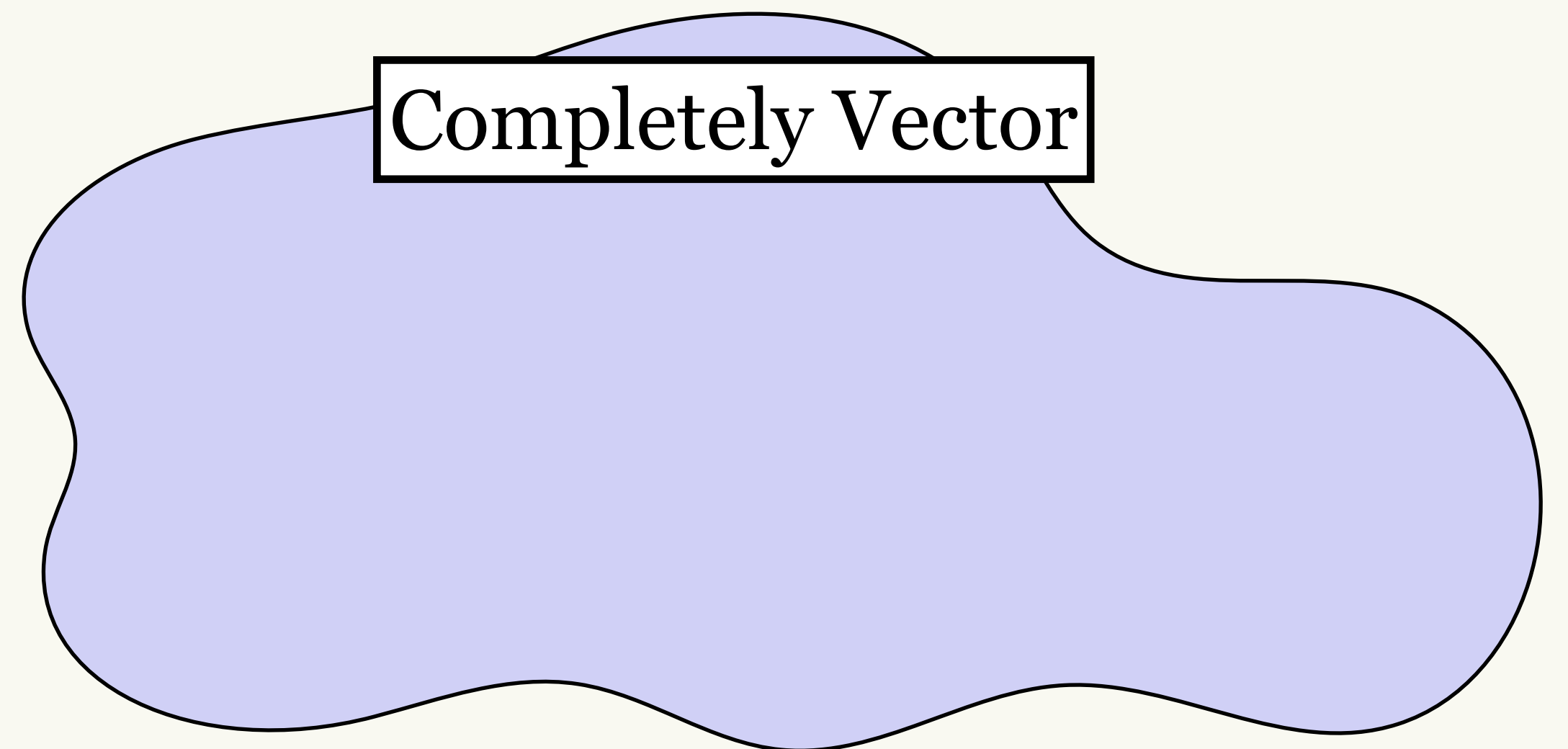
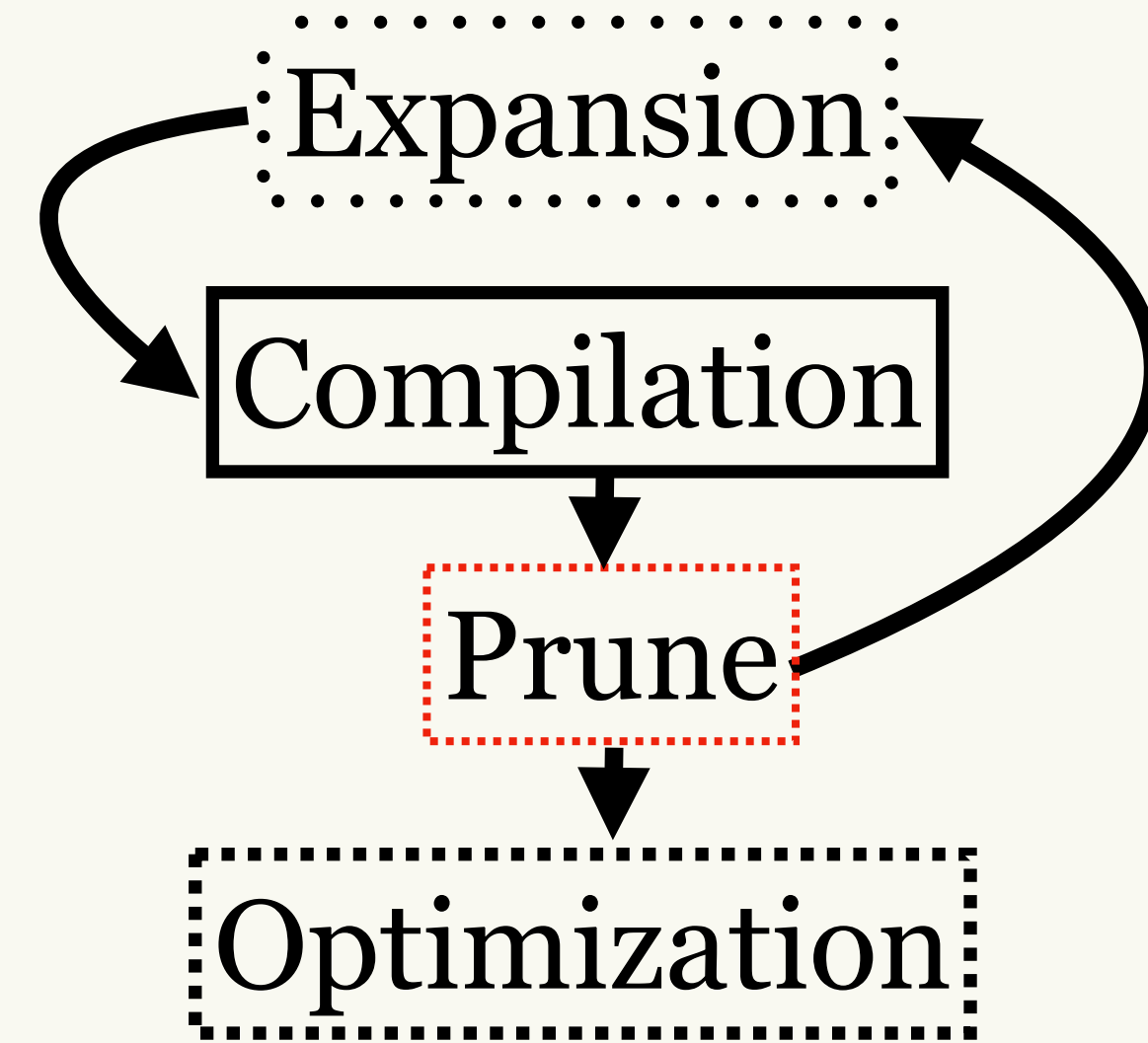
2. Pruning



1. Rule Phasing

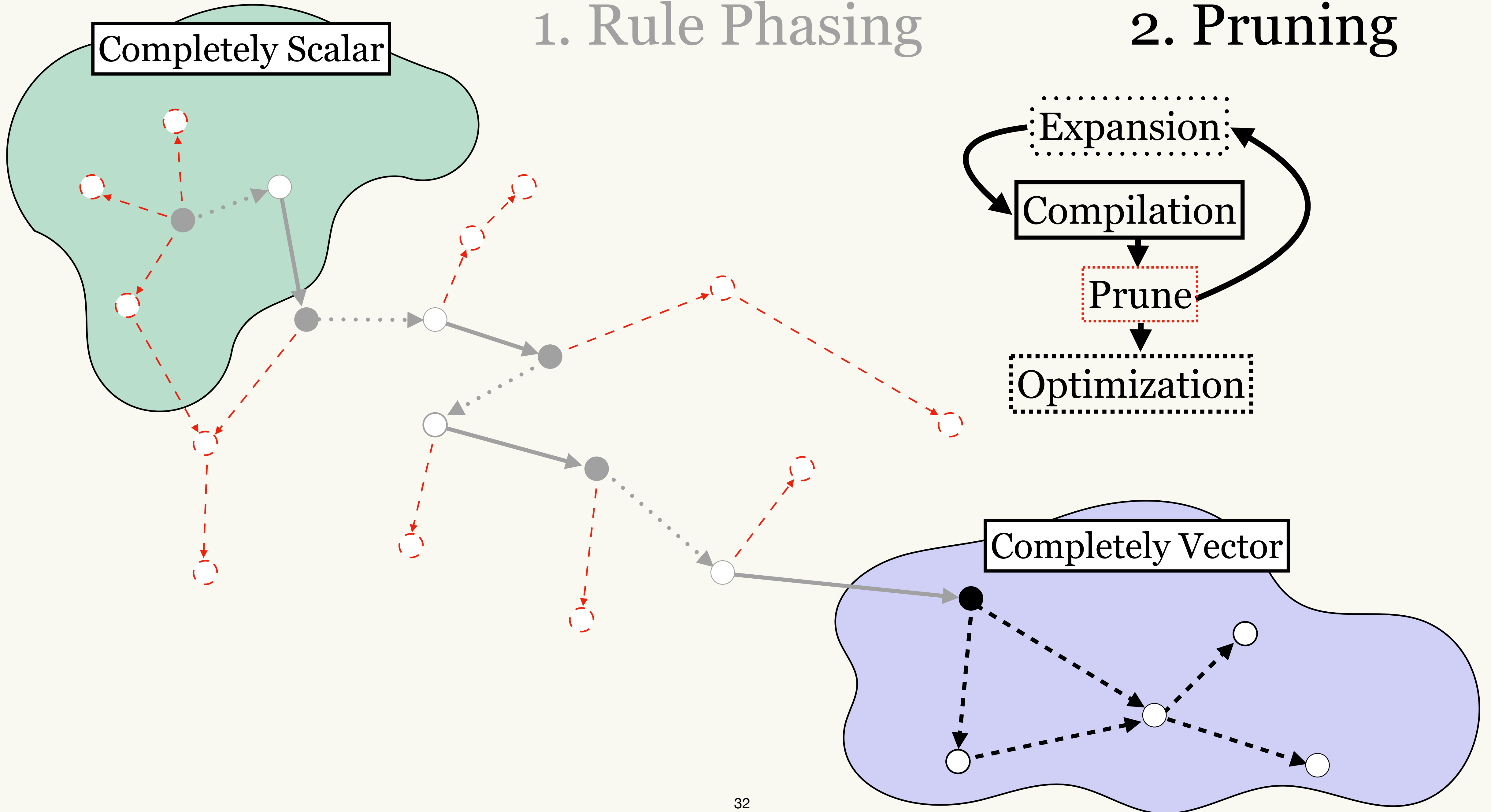


2. Pruning



1. Rule Phasing

2. Pruning



Isaria: Choosing Phases

Rewrite Rules

$(\text{Vec } (+ \ ?a \ ?b)) \iff (\text{VecAdd } (\text{Vec } ?a) (\text{Vec } ?b))$

$(\text{Vec } (* \ ?a \ ?b)) \iff (\text{VecMul } (\text{Vec } ?a) (\text{Vec } ?b))$

$(+ \ ?a \ ?b) \iff (+ \ ?b \ ?a)$

$(* \ ?a \ ?b) \iff (* \ ?b \ ?a)$

$(\text{VecAdd } ?b \ ?a) \iff (\text{VecAdd } ?a \ ?b)$

$(\text{VecMinus } ?b (\text{VecNeg } ?a)) \iff (\text{VecAdd } ?a \ ?b)$

$(\text{sgn } ?a) \iff (\text{sgn } (\text{sgn } ?a))$

$(\text{neg } (* \ ?b \ ?a)) \iff (* \ ?b (\text{neg } ?a))$

$(\text{VecMAC } ?c \ ?b \ ?a) \iff (\text{VecAdd } ?c (\text{VecMul } ?b \ ?a))$

$(\text{VecMul } ?b \ ?a) \iff (\text{VecMul } ?a \ ?b)$

$(/ \ 0 \ ?a) \iff (/ \ 0 (\text{sgn } ?a))$

$(\text{VecNeg } (\text{VecMul } ?b \ ?a)) \iff (\text{VecMul } ?a (\text{VecNeg } ?b))$

⋮

ISA
Cost
Model

Expansion

Compilation

Optimization

Isaria: Choosing Phases

ISA
Cost
Model

Expansion

$$(+ \ ?a \ ?b) \iff (+ \ ?b \ ?a)$$

$$(* \ ?a \ ?b) \iff (* \ ?b \ ?a)$$

$$(\text{sgn } ?a) \iff (\text{sgn } (\text{sgn } ?a))$$

$$(\text{neg } (* \ ?b \ ?a)) \iff (* \ ?b \ (\text{neg } ?a))$$

$$(/ \ 0 \ ?a) \iff (/ \ 0 \ (\text{sgn } ?a))$$

Compilation

$$(\text{Vec } (+ \ ?a \ ?b)) \implies (\text{VecAdd } (\text{Vec } ?a) (\text{Vec } ?b))$$

$$(\text{Vec } (* \ ?a \ ?b)) \implies (\text{VecMul } (\text{Vec } ?a) (\text{Vec } ?b))$$

Optimization

$$(\text{VecAdd } ?b \ ?a) \iff (\text{VecAdd } ?a \ ?b)$$

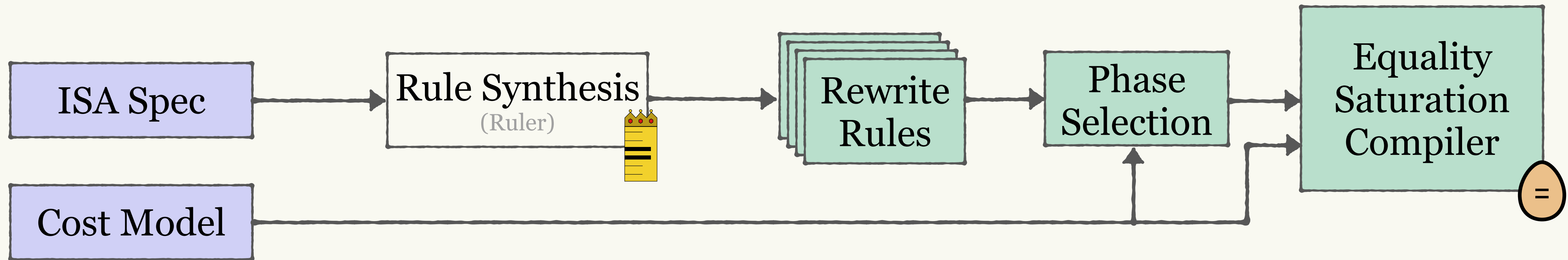
$$(\text{VecMinus } ?b \ (\text{VecNeg } ?a)) \iff (\text{VecAdd } ?a \ ?b)$$

$$(\text{VecMAC } ?c \ ?b \ ?a) \iff (\text{VecAdd } ?c \ (\text{VecMul } ?b \ ?a))$$

$$(\text{VecMul } ?b \ ?a) \iff (\text{VecMul } ?a \ ?b)$$

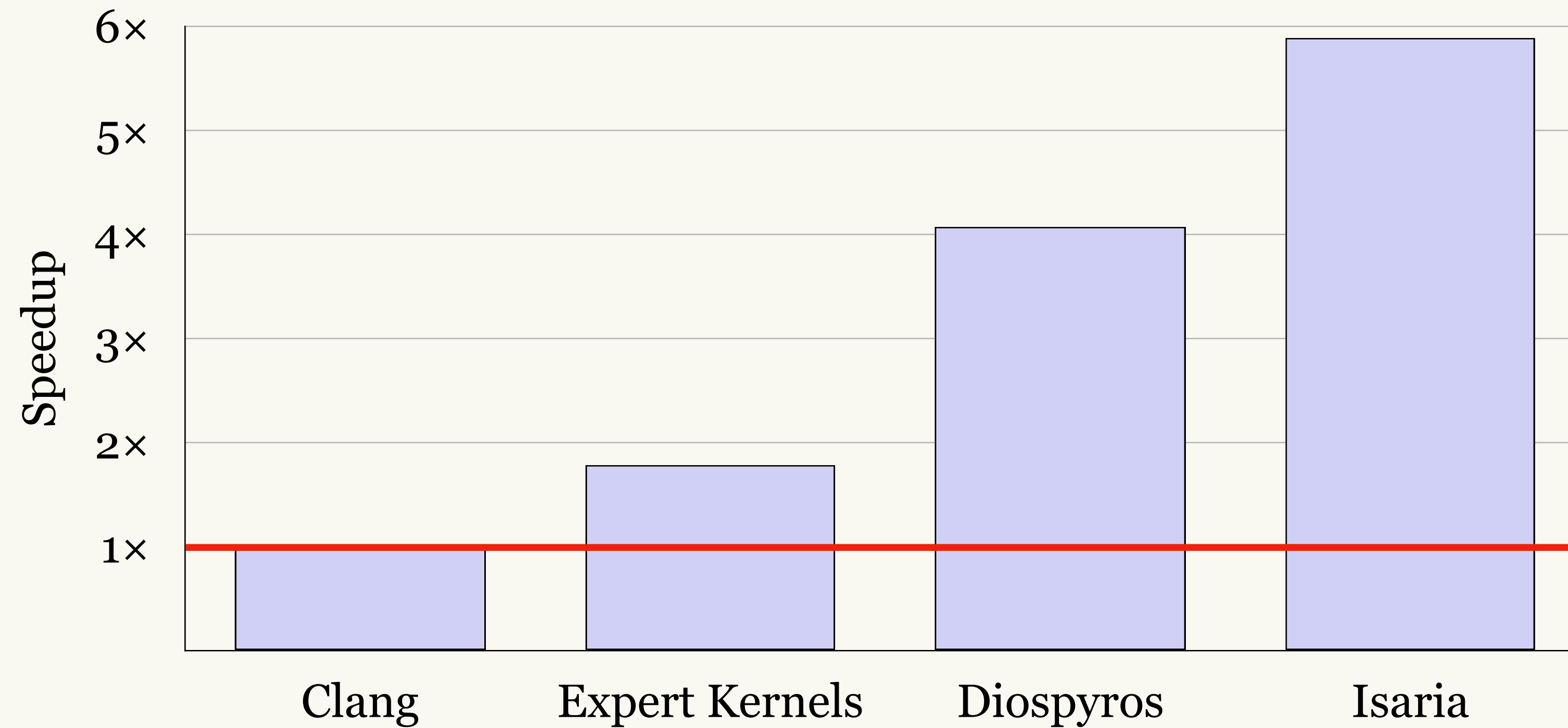
$$(\text{VecNeg } (\text{VecMul } ?b \ ?a)) \iff (\text{VecMul } ?a \ (\text{VecNeg } ?b))$$

Isaria

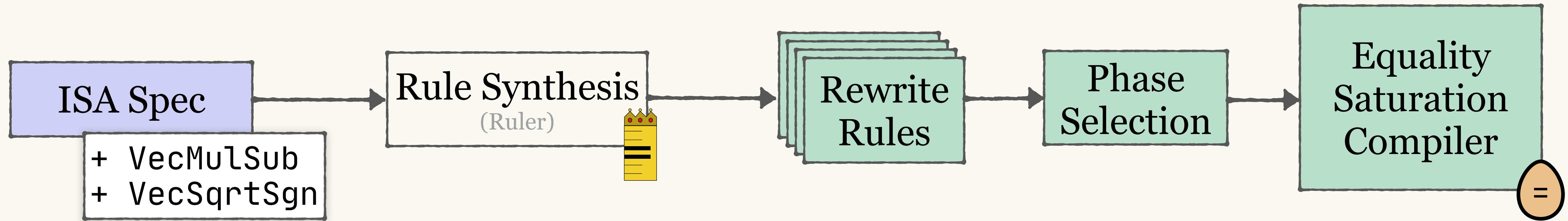


How do we compare against handwritten compilers?

Geo-mean Speedup over Clang Auto-vectorization



Case Study



	VecMulSub	No VecMulSub
VecSqrtSgn	2.0%	1.7%
No VecSqrtSgn	0.5%	-

Performance improvement
for QR-Decomposition

Thanks!

